

# Sample size requirements to compare development between unbalanced subgroups in latent growth models

---

Mariëlle Zondervan-Zwijnenburg<sup>1</sup>,  
Margot Peeters<sup>2</sup>, Wilma Vollebergh<sup>2</sup>, & Rens van de Schoot<sup>1,3</sup>

<sup>1</sup>Utrecht University, Department of Methodology & Statistics

<sup>2</sup>Utrecht University, Department of Child and Adolescent Studies

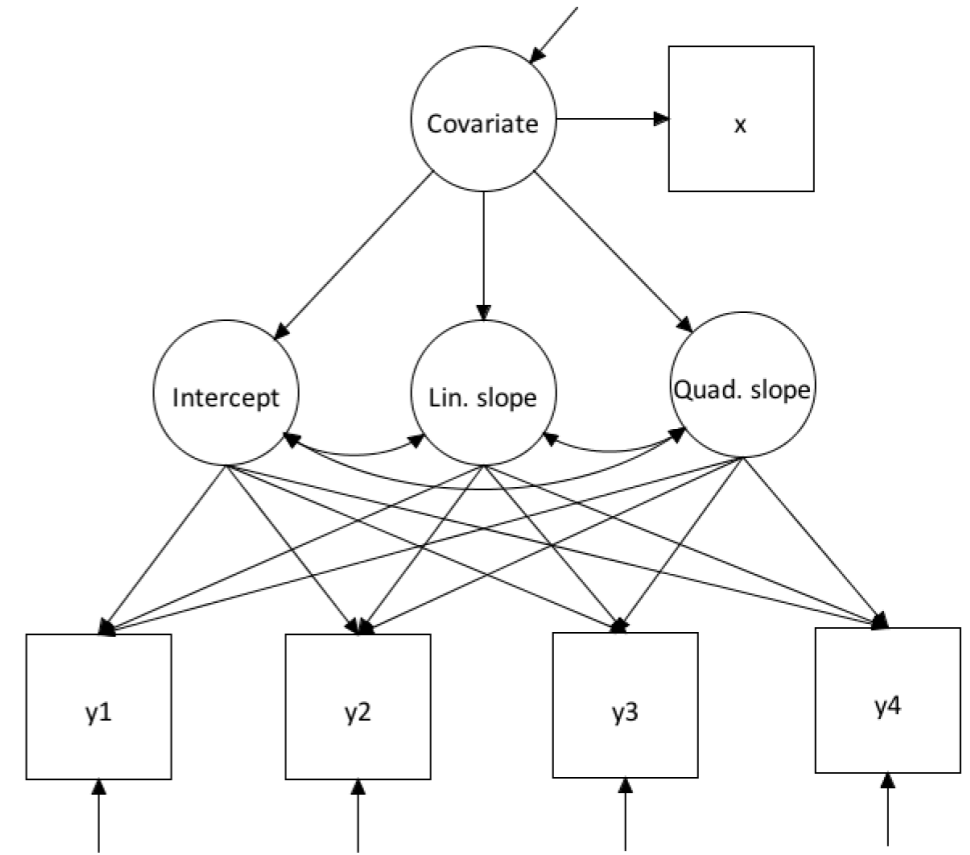
<sup>3</sup>North-West University, Optentia Research Focus Area

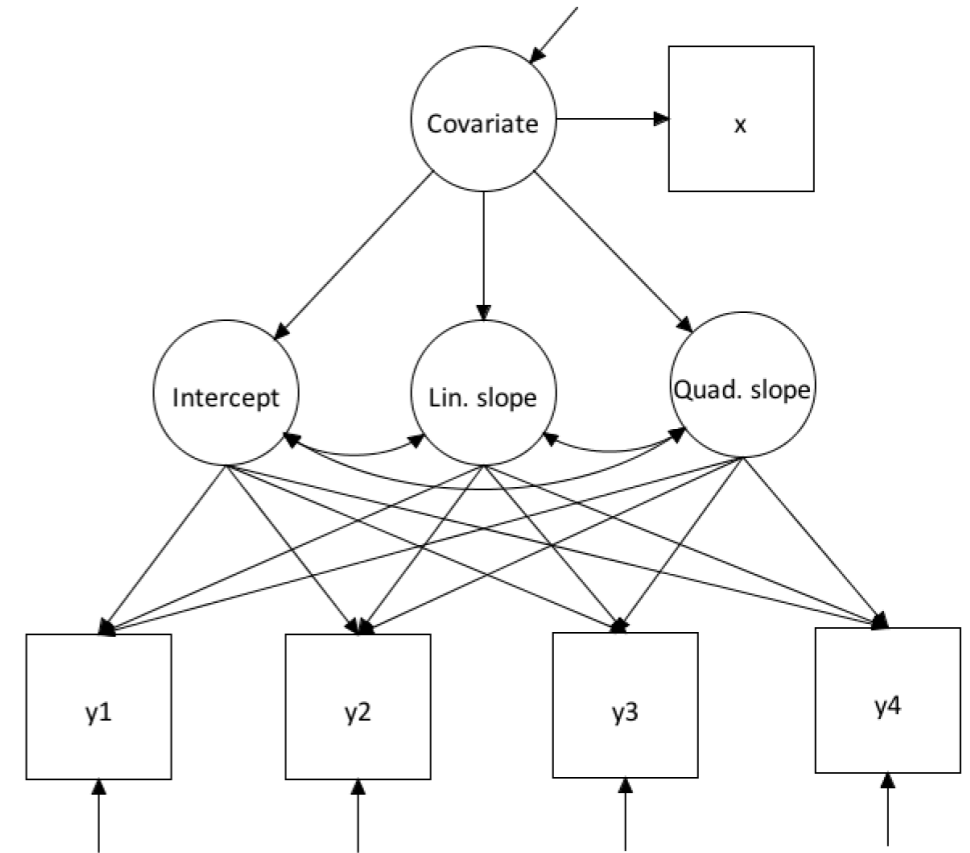
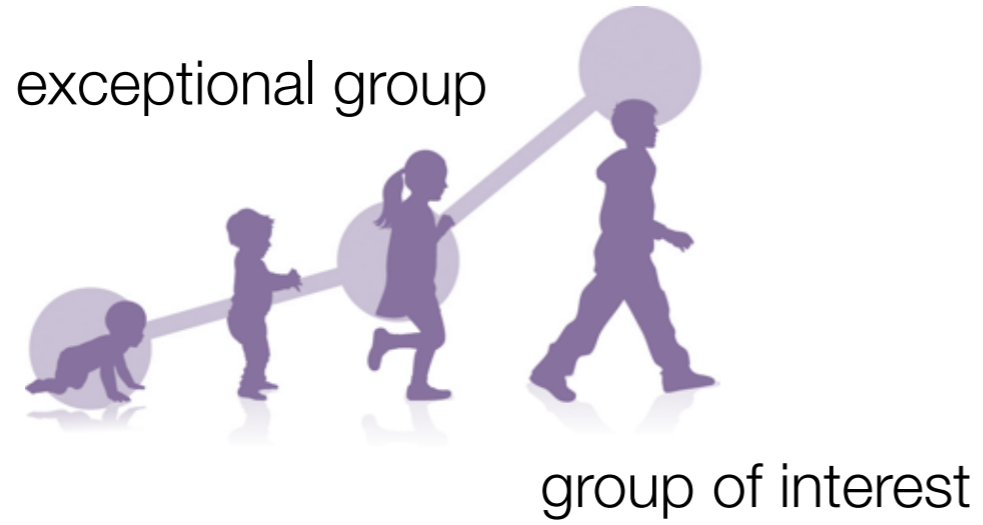
# Outline

---

1. Introduction
2. What do we know?
3. Model
4. Simulation design
5. Syntax
6. Results
7. Conclusion
8. To be continued







typically developing group

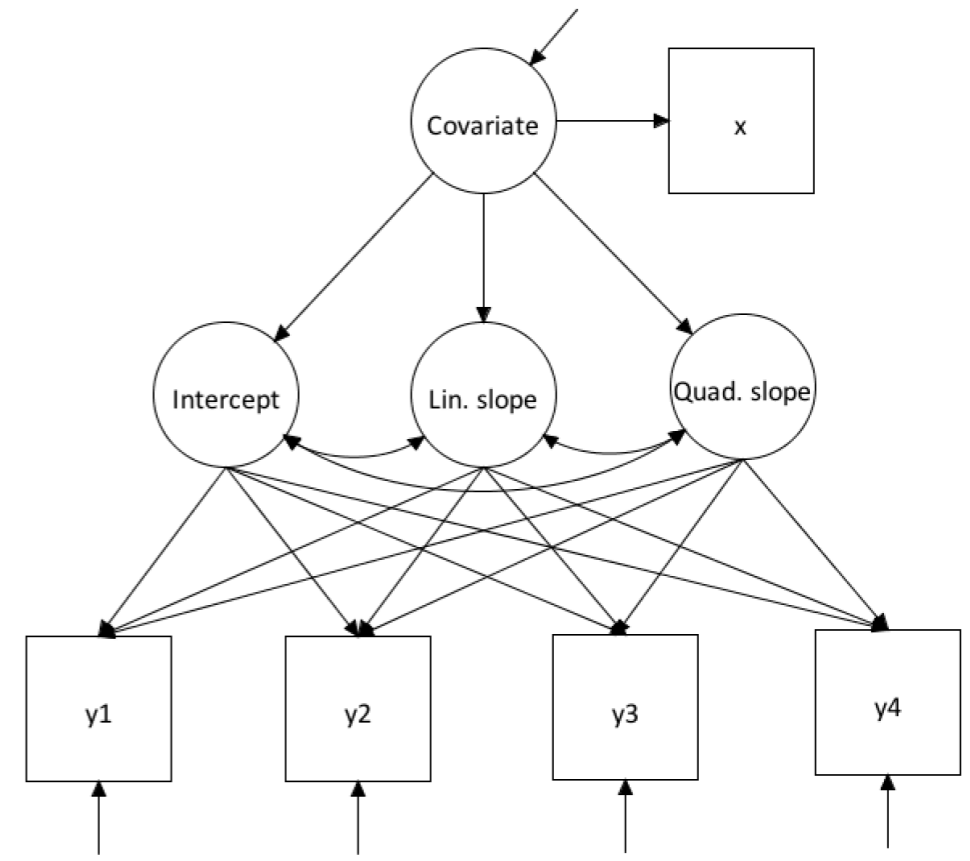


reference group

exceptional group



group of interest



# What do we know?

---

- Maximum Likelihood (ML) estimation
- Bayesian estimation (default settings)
- Bayesian estimation with informative priors

# What do we know?

---

- Maximum Likelihood (ML) estimation

small sample:                    +- 50 participants = little bias, but low power<sup>1</sup>, Type I error > .05<sup>2,3</sup>

unbalanced samples:    keeping everything else constant: balanced is better for power<sup>4</sup>

- Bayesian estimation (default prior settings)
  
- Bayesian estimation with informative priors

<sup>1</sup>Tolvanen (2000), <sup>2</sup>Meuleman & Billiet (2009), <sup>3</sup>Maas & Hox (2001), <sup>4</sup>Muthén & Curran (1997)



# What do we know?

---

- Maximum Likelihood (ML) estimation

small sample:                   +- 50 participants = little bias, but low power<sup>1</sup>, Type I error > .05<sup>2,3</sup>

unbalanced samples:   keeping everything else constant: balanced is better for power<sup>4</sup>

- Bayesian estimation (default prior settings)

small sample:                   +- 20 participants = little bias, but low power<sup>5</sup>

unbalanced samples:   ?

- Bayesian estimation with informative priors

<sup>1</sup>Tolvanen (2000), <sup>2</sup>Meuleman & Billiet (2009), <sup>3</sup>Maas & Hox (2001), <sup>4</sup>Muthén & Curran (1997),

<sup>5</sup>Hox, Van de Schoot, & Matthijsse (2012)

# What do we know?

---

- Maximum Likelihood (ML) estimation

small sample:                   +- 50 participants = little bias, but low power<sup>1</sup>, Type I error > .05<sup>2,3</sup>

unbalanced samples:   keeping everything else constant: balanced is better for power<sup>4</sup>

- Bayesian estimation (default prior settings)

small sample:                   +- 20 participants = little bias, but low power<sup>5</sup>

unbalanced samples:   ?

- Bayesian estimation with informative priors

small sample:                   +- ? participants → expectation: fewer participants required<sup>6,7</sup>

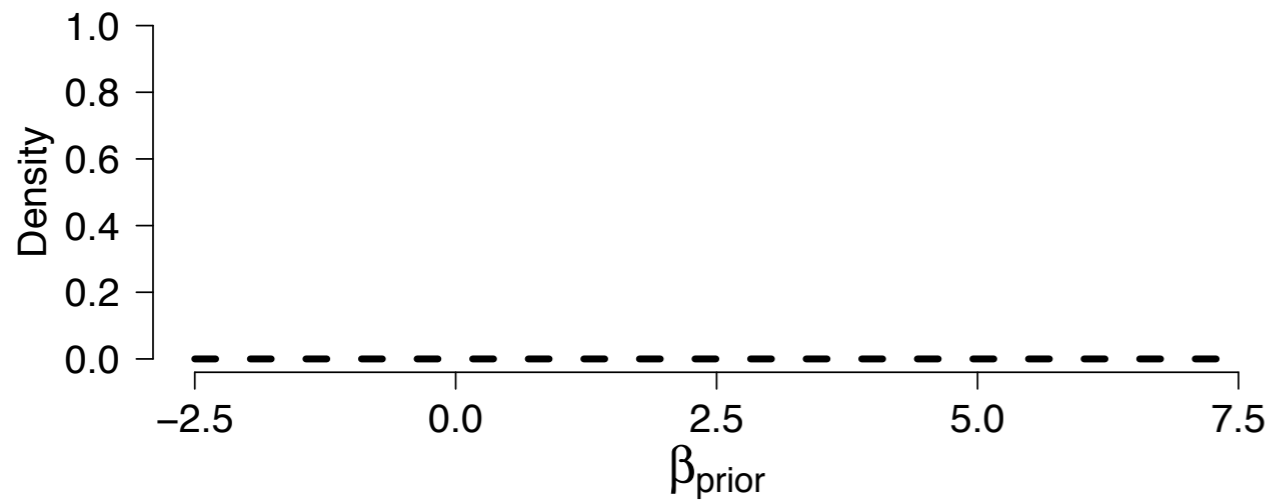
unbalanced samples:   ?

<sup>1</sup>Tolvanen (2000), <sup>2</sup>Meuleman & Billiet (2009), <sup>3</sup>Maas & Hox (2001), <sup>4</sup>Muthén & Curran (1997),

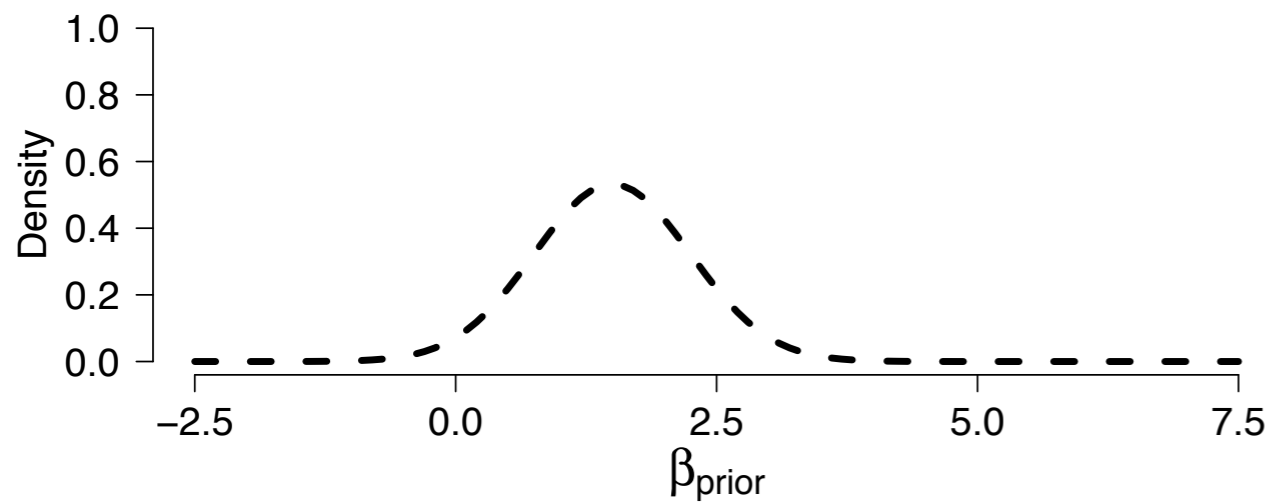
<sup>5</sup>Hox, Van de Schoot, & Matthijsse (2012), <sup>6</sup>Lee & Song (2004), <sup>7</sup>Depaoli (2013)

# Prior information

---



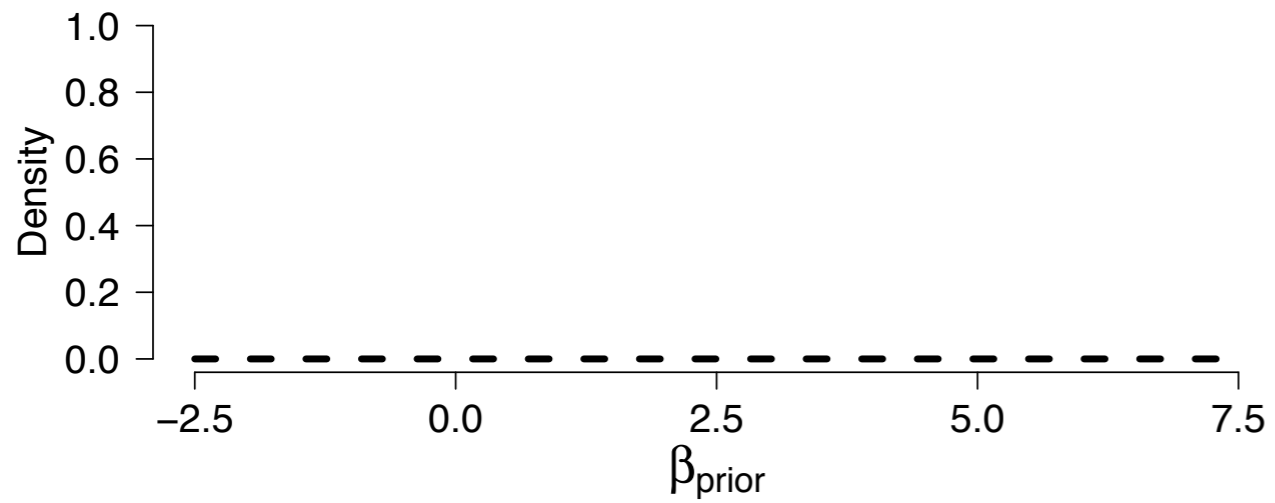
uninformative



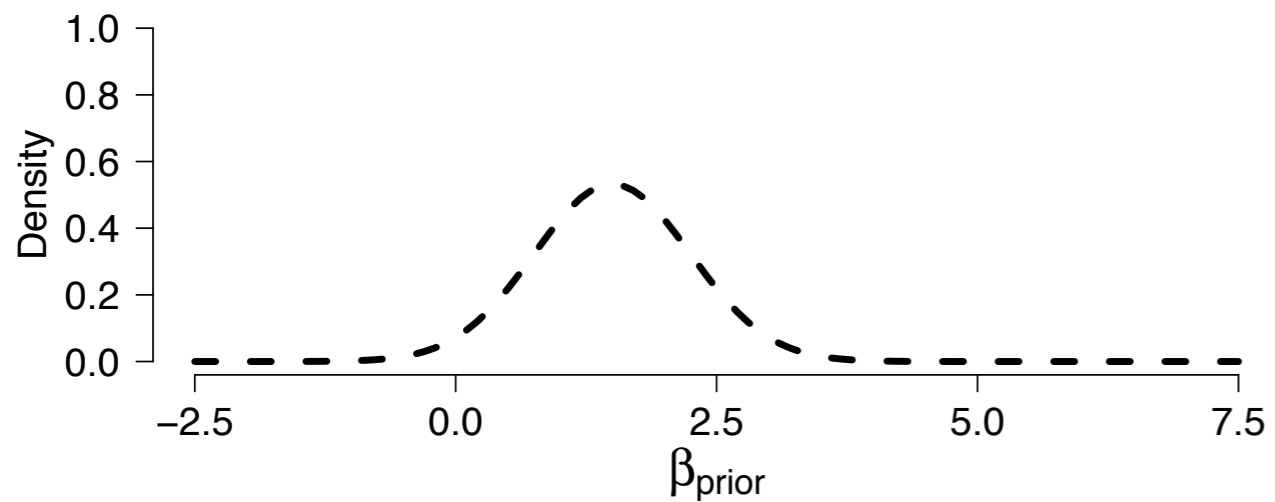
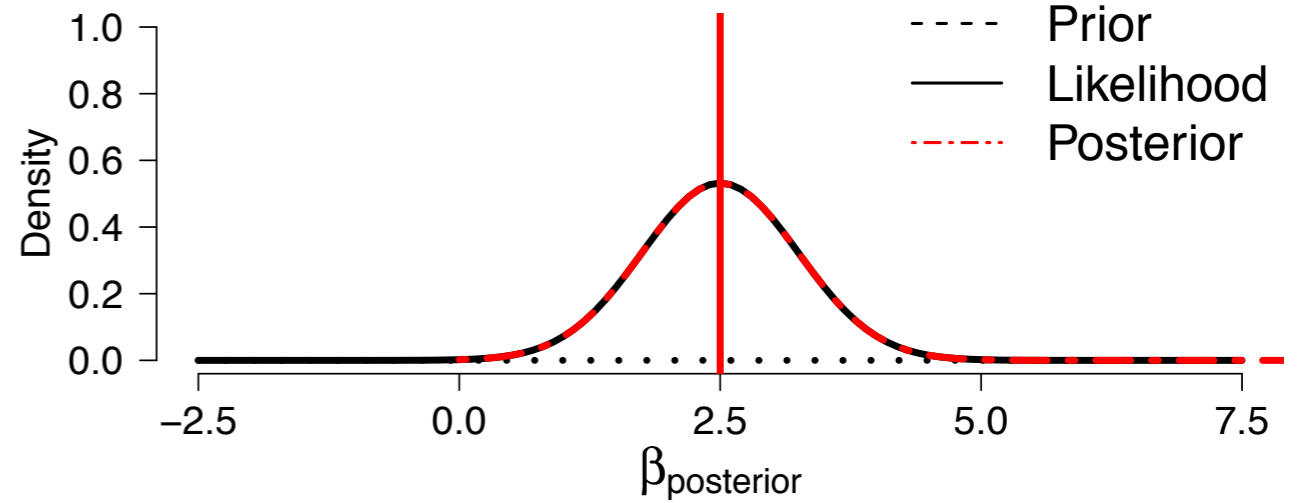
informative

# Prior information

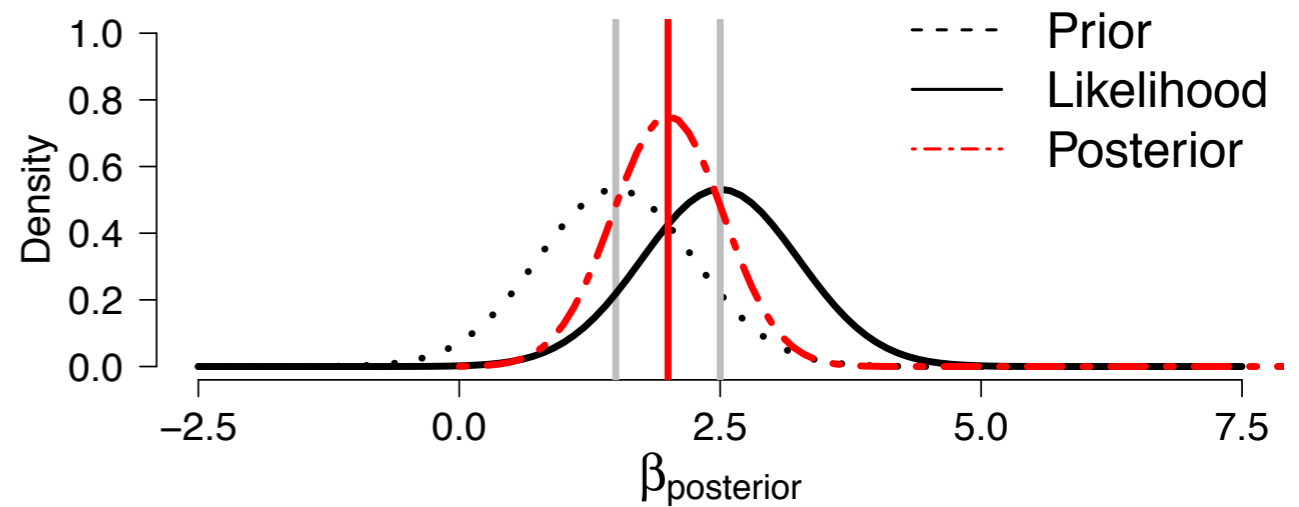
---



uninformative

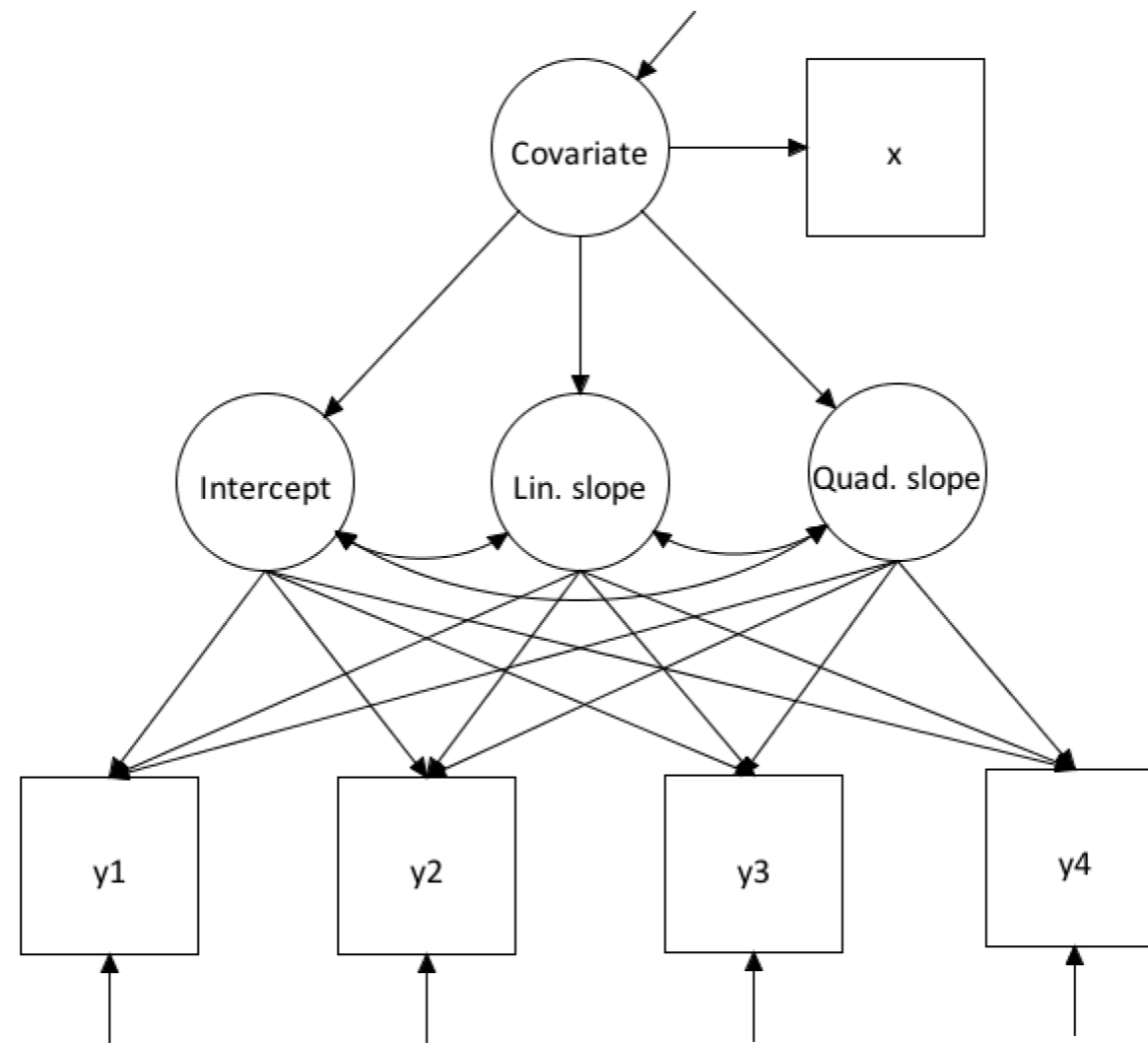


informative

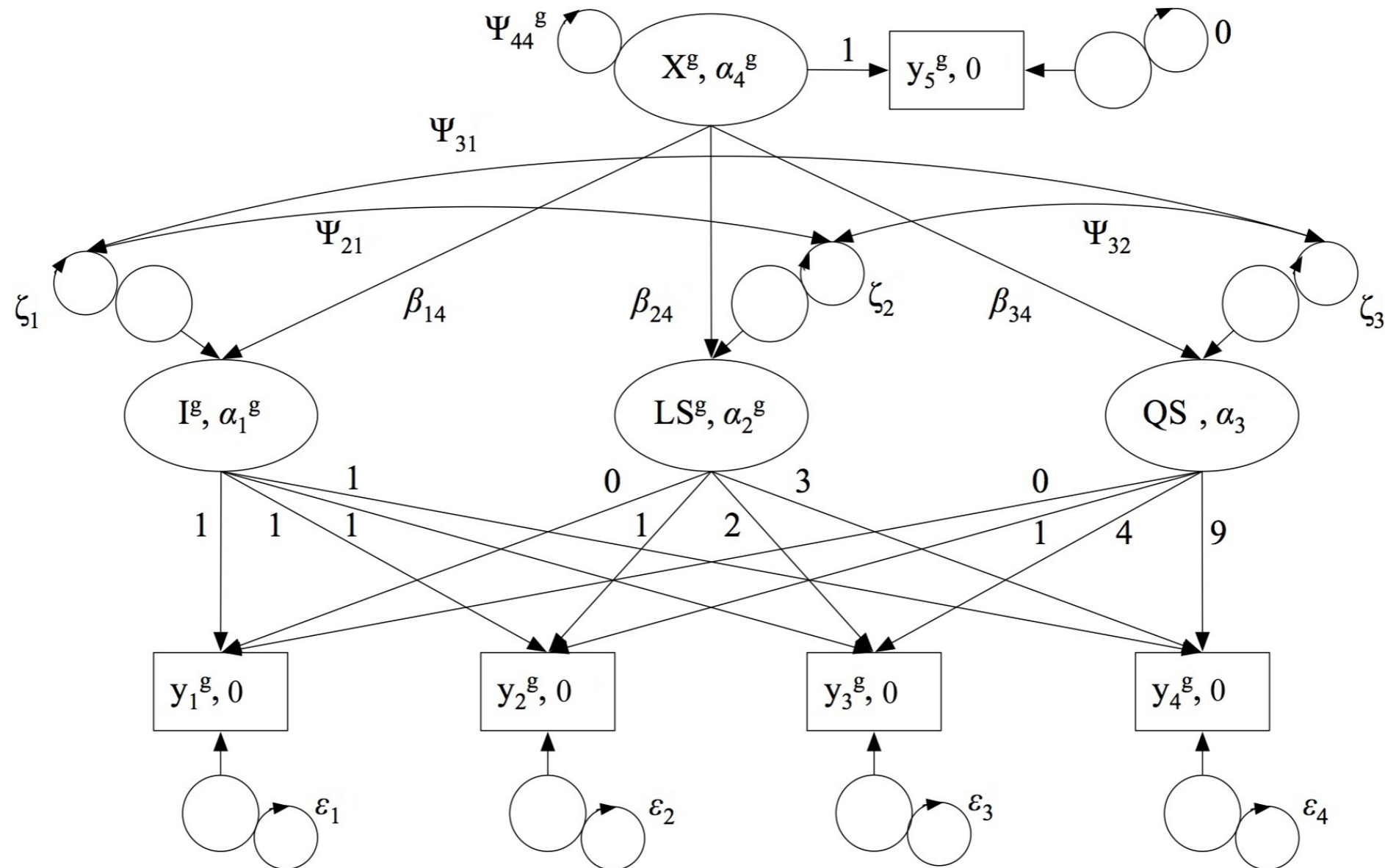


# The latent growth model in the Mplus Diagrammer

---



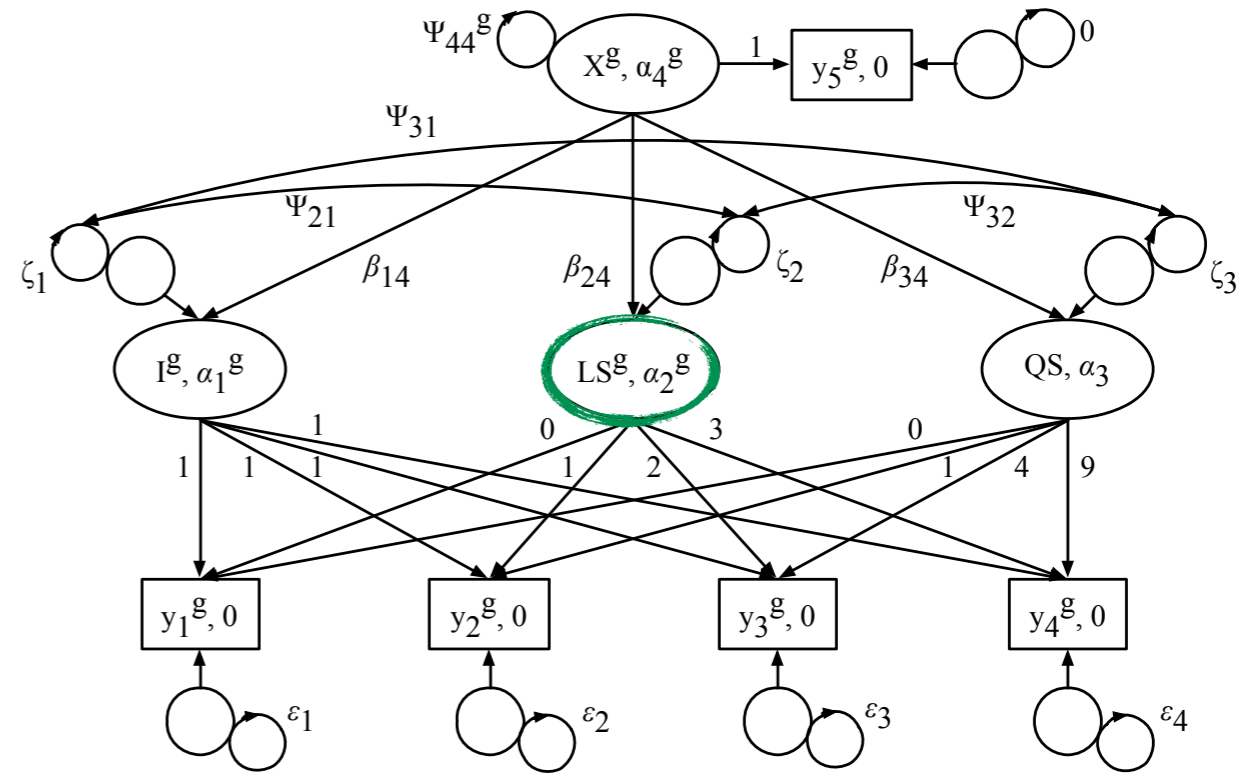
# The multiple group latent growth model in Mplus



# Simulation design (1)

Focus

$$\mathbf{a}_2^1 - \mathbf{a}_2^2 = \Delta \mathbf{a}_2$$

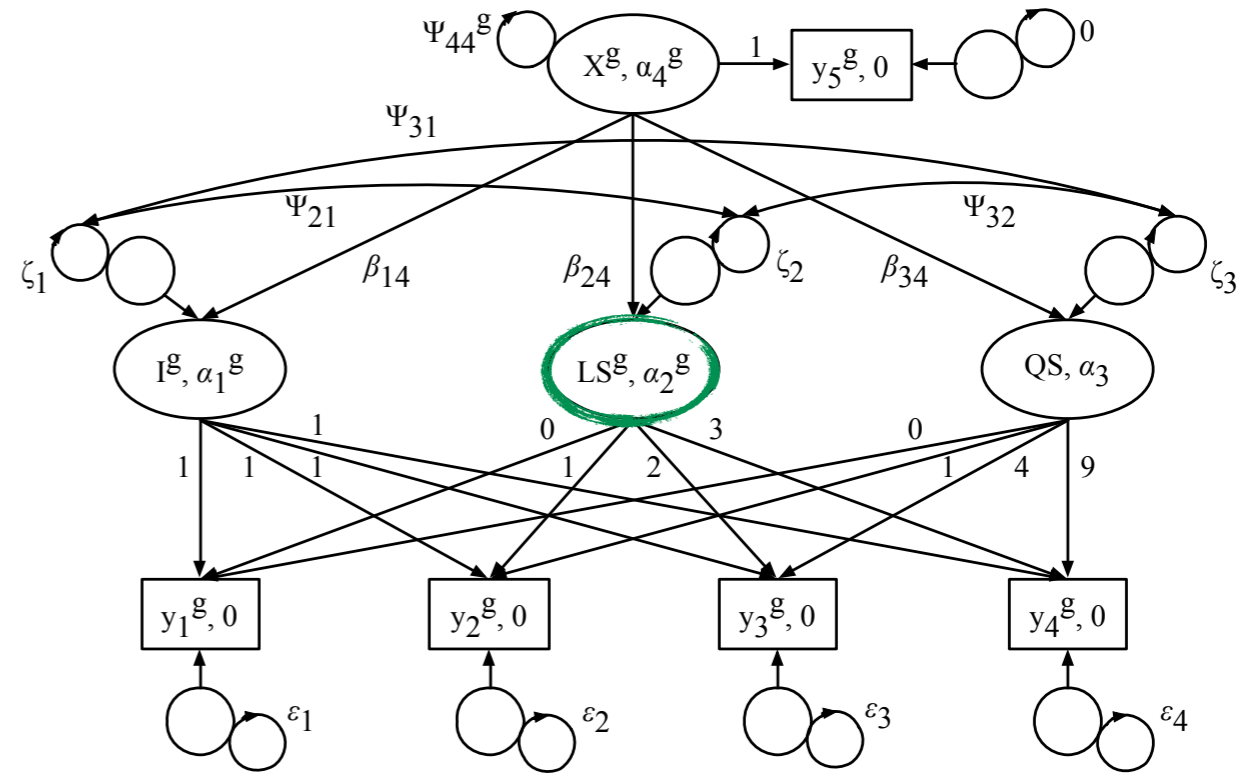


# Simulation design (1)

Focus

$$\mathbf{a}_2^1 - \mathbf{a}_2^2 = \Delta \mathbf{a}_2$$

Factors





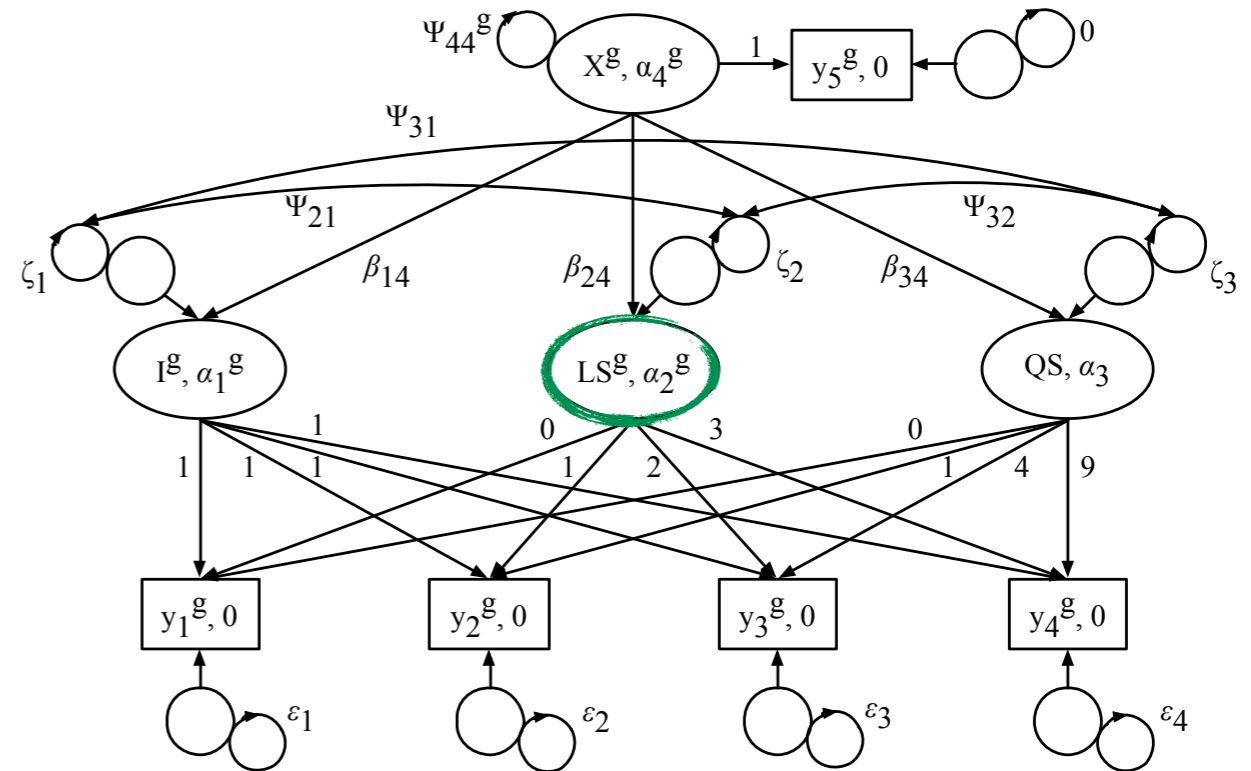
# Simulation design (1)

Focus

$$\mathbf{a}_2^1 - \mathbf{a}_2^2 = \Delta \mathbf{a}_2$$

Factors

- $n$  exceptional group



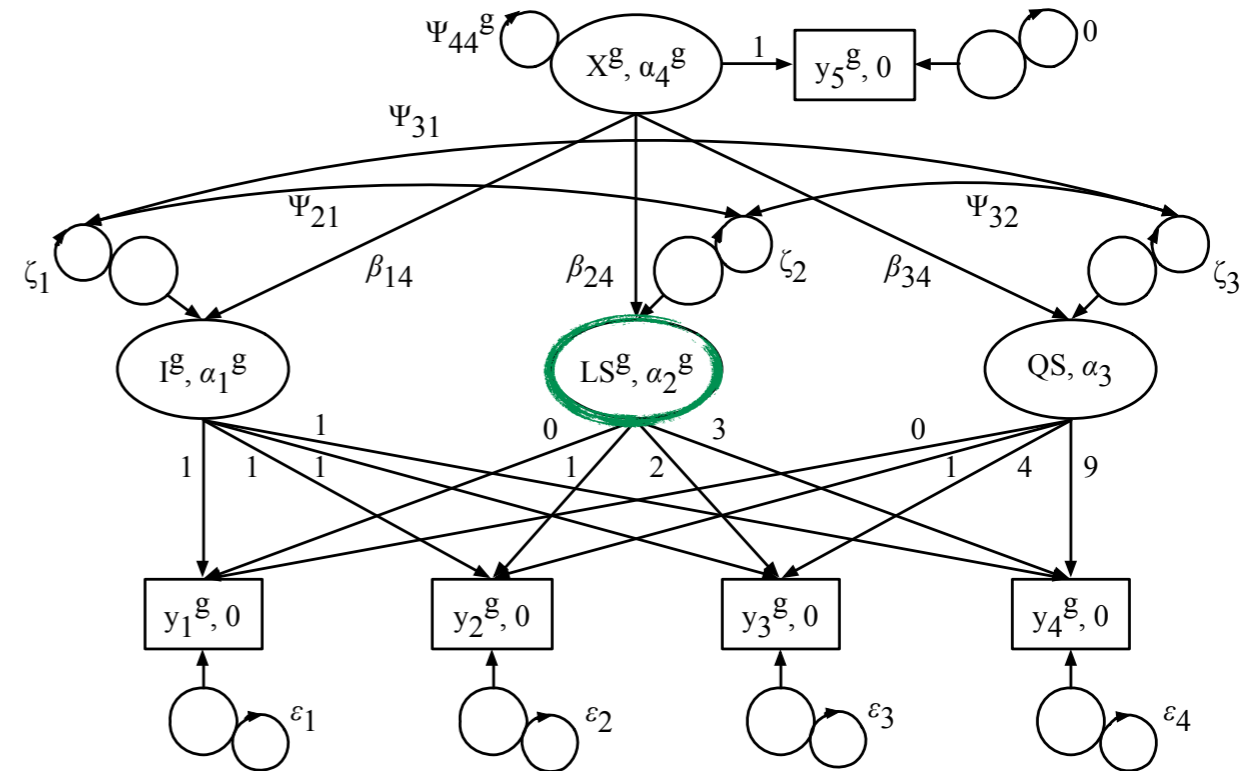
# Simulation design (1)

Focus

$$\mathbf{a}_2^1 - \mathbf{a}_2^2 = \Delta \mathbf{a}_2$$

Factors

- $n$  exceptional group
- $n$  reference group



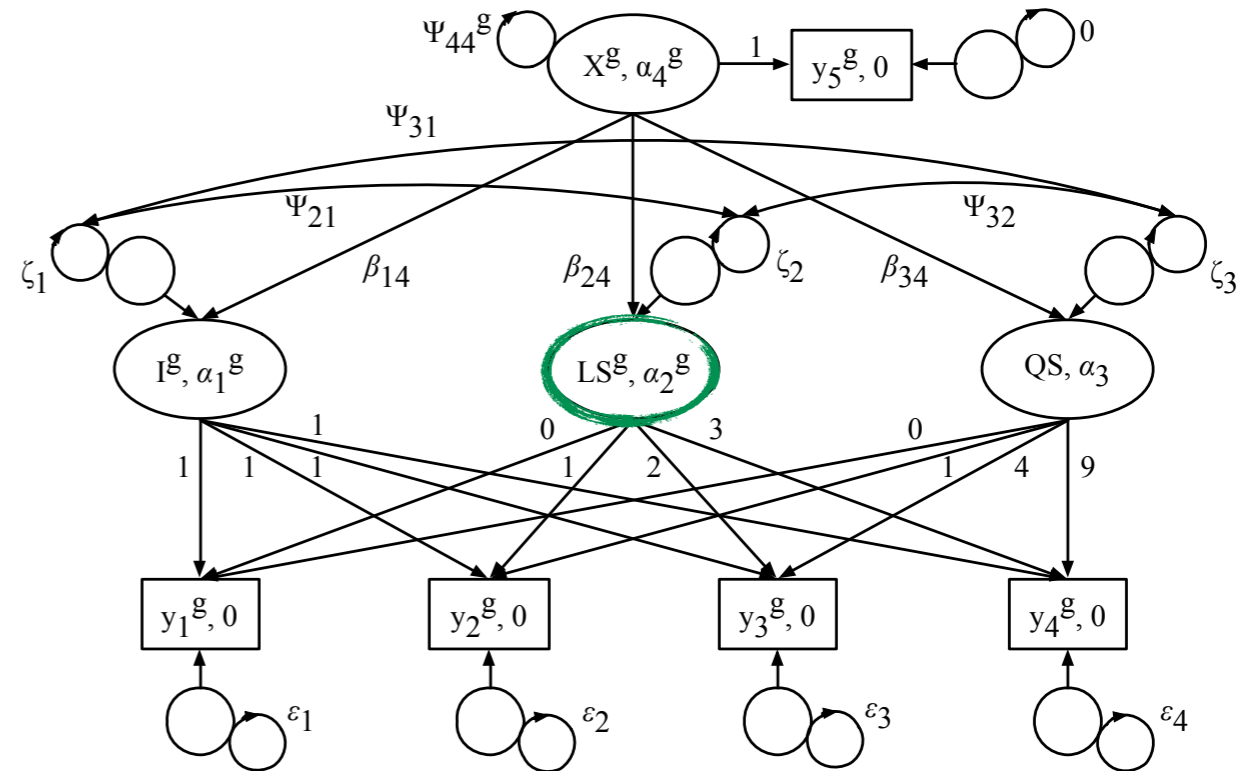
# Simulation design (1)

Focus

$$\mathbf{a}_2^1 - \mathbf{a}_2^2 = \Delta \mathbf{a}_2$$

Factors

- $n$  exceptional group
- $n$  reference group
- (ratio exceptional:reference)



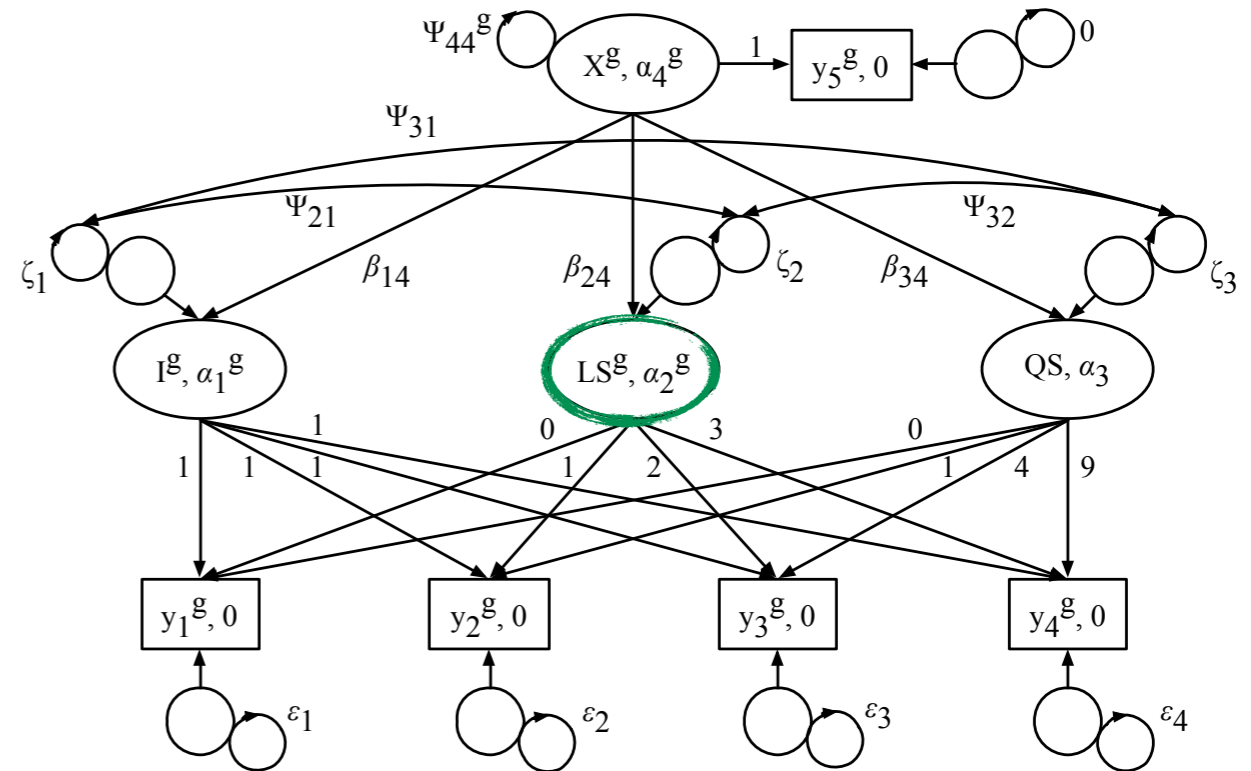
# Simulation design (1)

Focus

$$\mathbf{a}_2^1 - \mathbf{a}_2^2 = \Delta \mathbf{a}_2$$

Factors

- $n$  exceptional group
- $n$  reference group
- (ratio exceptional:reference)
- estimation method & settings



# Simulation design (1)

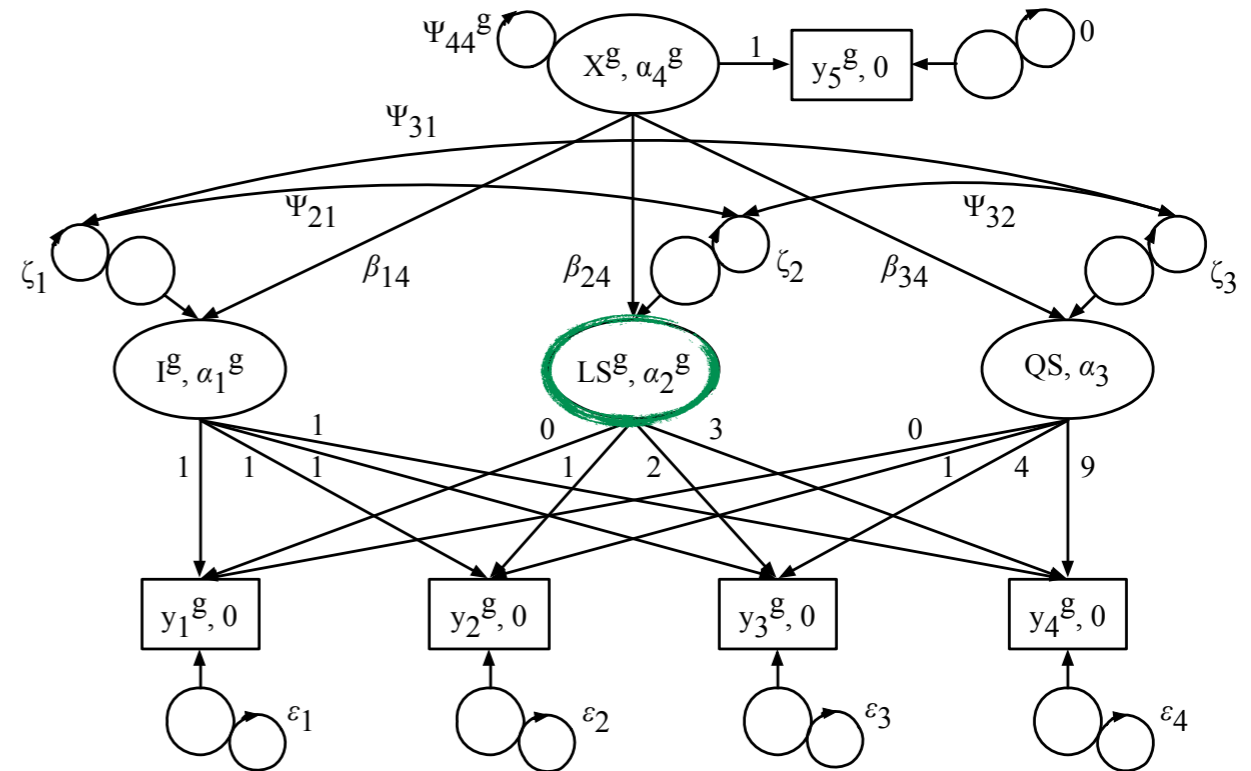
Focus

$$\mathbf{a}_2^1 - \mathbf{a}_2^2 = \Delta \mathbf{a}_2$$

Factors

- $n$  exceptional group
- $n$  reference group
- (ratio exceptional:reference)
- estimation method & settings

$n$  exceptional group = 5, 10, 25, 50



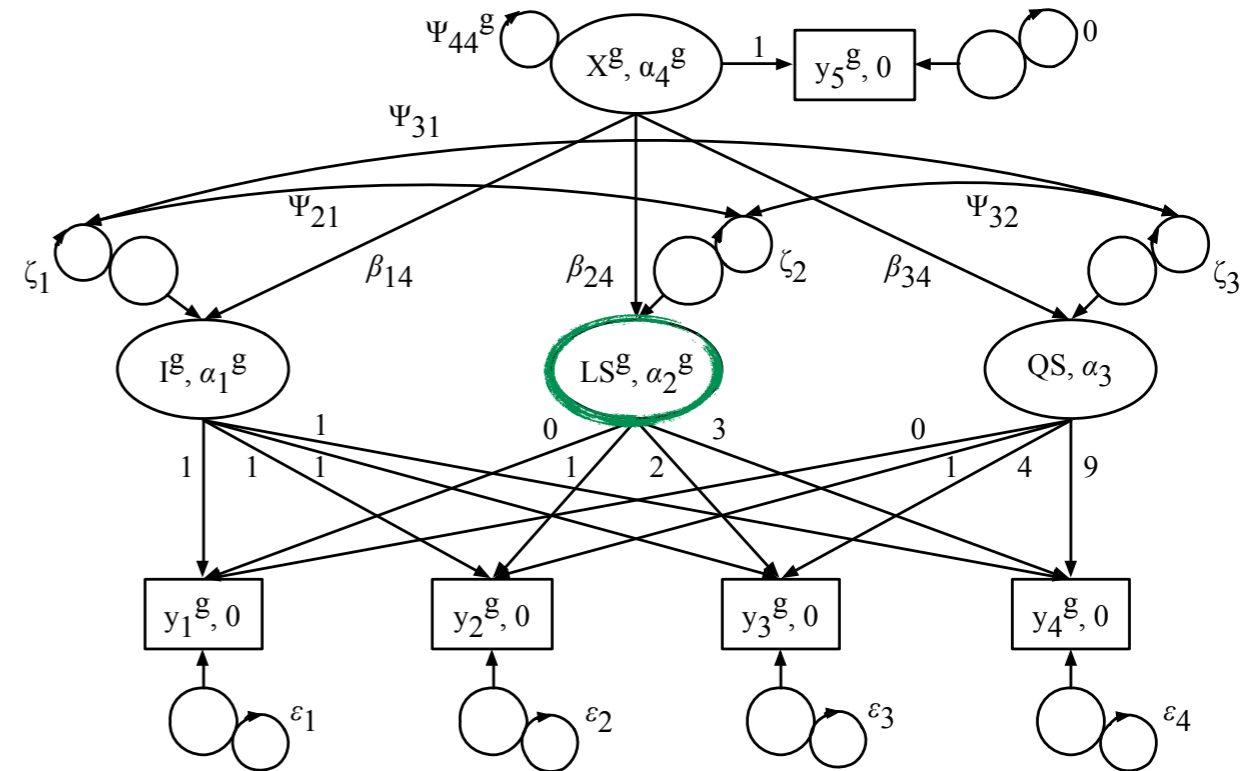
# Simulation design (1)

Focus

$$\mathbf{a}_2^1 - \mathbf{a}_2^2 = \Delta \mathbf{a}_2$$

Factors

- $n$  exceptional group
- $n$  reference group
- (ratio exceptional:reference)
- estimation method & settings



$n$  exceptional group = 5, 10, 25, 50

$n$  reference group = 50, 100, 200, 500, 1,000, 2,000, 5,000, 10,000

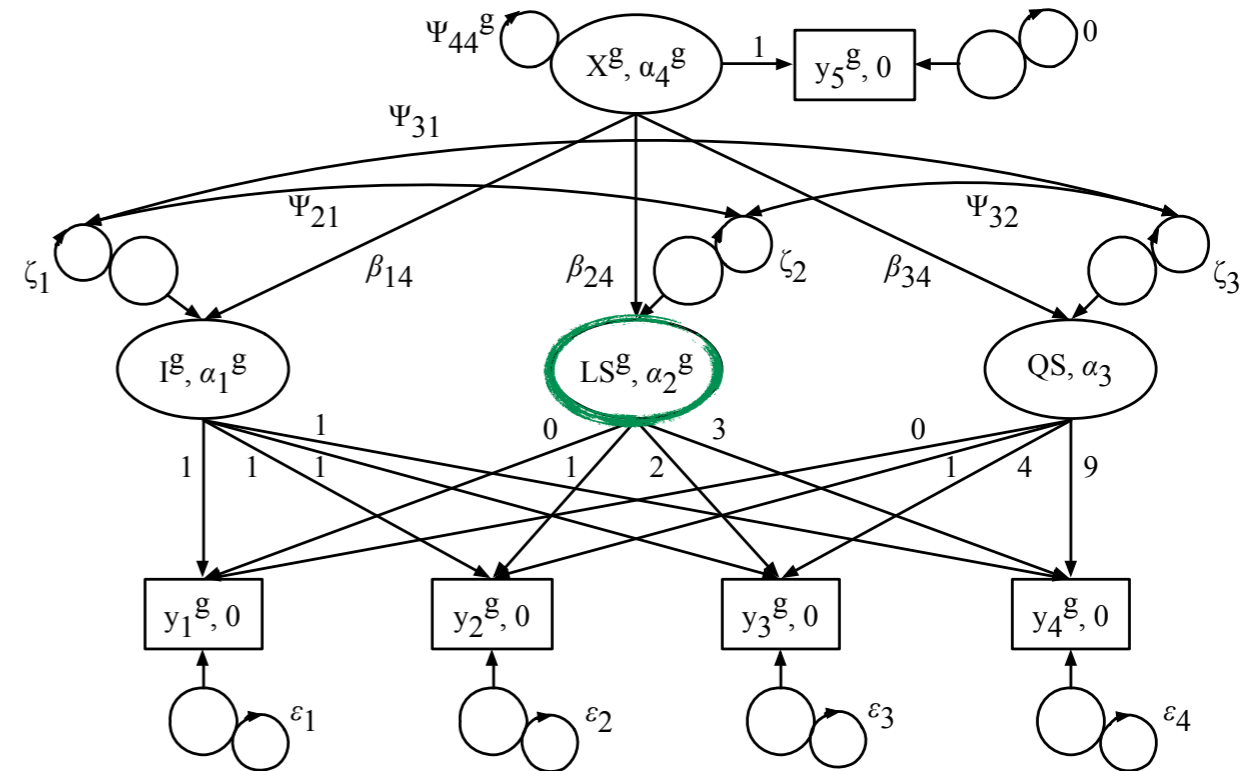
# Simulation design (1)

Focus

$$\mathbf{a}_2^1 - \mathbf{a}_2^2 = \Delta \mathbf{a}_2$$

Factors

- $n$  exceptional group
- $n$  reference group
- (ratio exceptional:reference)
- estimation method & settings



$n$  exceptional group = 5, 10, 25, 50

$n$  reference group = 50, 100, 200, 500, 1,000, 2,000, 5,000, 10,000

ratio = 1:1 - 1:2,000

# Simulation design (2)

---

## Estimation method and settings

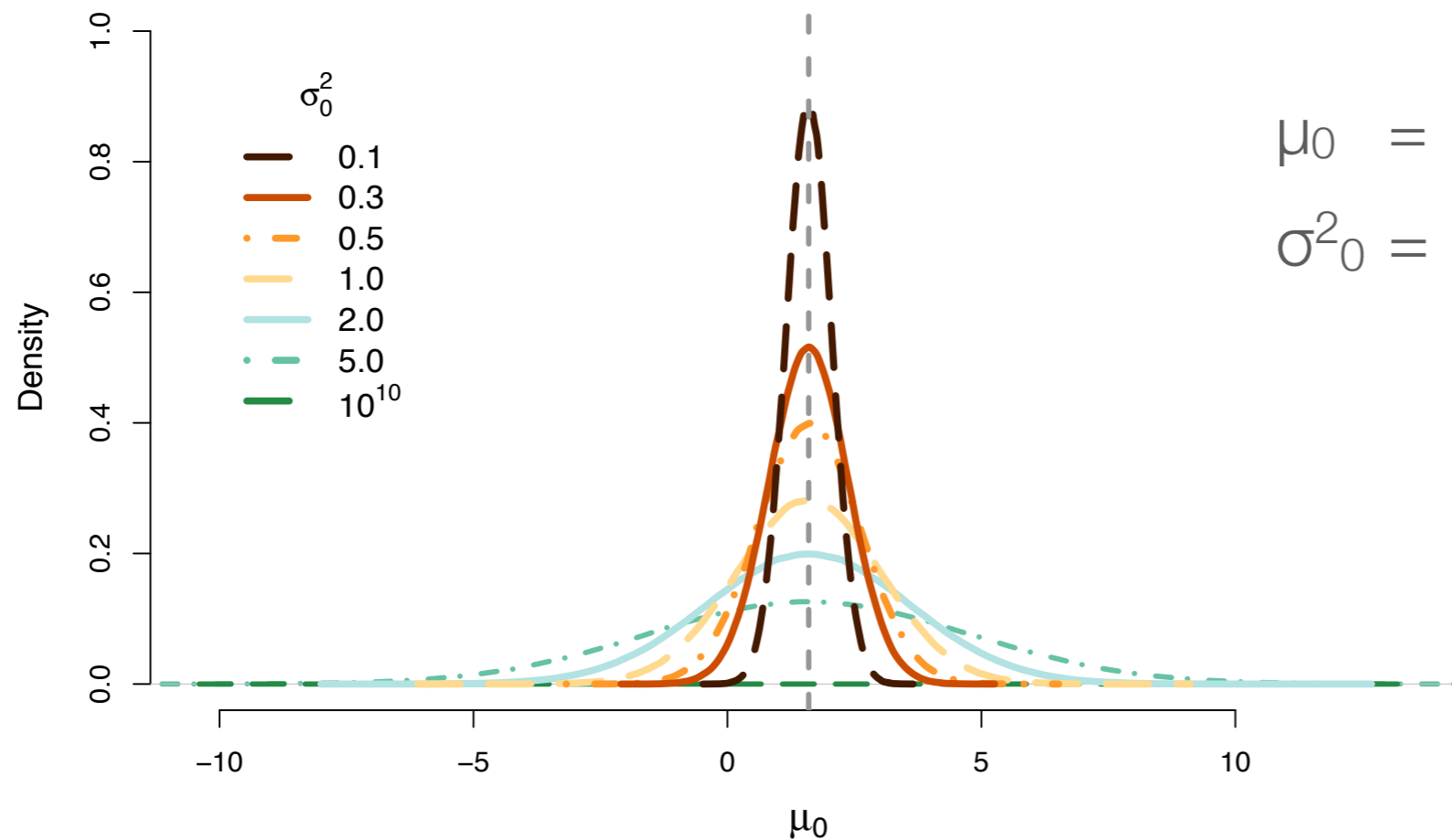
- ML(R) estimation
- Bayes with default priors
- Bayes with informative priors on  $\mathbf{a}_1^g, \mathbf{a}_2^g, \mathbf{a}_3 \sim N(\mu_0, \sigma^2_0)$



# Simulation design (2)

## Estimation method and settings

- ML(R) estimation
- Bayes with default priors
- Bayes with informative priors on  $\mathbf{a}_1^g, \mathbf{a}_2^g, \mathbf{a}_3 \sim N(\mu_0, \sigma_0^2)$



$\mu_0$  = population value

$\sigma_0^2$  =  $(10^{10}), 5, 2, 1, 0.5, 0.3, 0.1$

# Simulation design (3)

---

## *Cells*

4 (exceptional group sample sizes)

x8 (reference group sample sizes) = 32 sample size settings

x8 (estimation settings) = 256 cells

- Mplus 7.11 (Muthén & Muthén, 1998-2012)
- R-package MplusAutomation (Hallquist, 2013)

# Syntax data generation (32,000 data files)

---

```
[[init]]
iterators = nobsmmin nobsmmax;

nobsmmin = 5 10 25 50;
nobsmmax = 50 100 200 500 1000 2000 5000 10000;
filename = "[[nobsmmin]]-[[nobsmmax]].inp";

outputDirectory = "C:/Sim/S[[nobsmmin]]/data";
[[/init]]
```

TITLE: Linear Growth MC

```
MONTECARLO:
NAMES = y1-y4 qft;
!y1-y4 = cognition, qft = alcohol use
count = qft;
generate = qft(c);
ngroups = 2;
nobs = [[nobsmmax]] [[nobsmmin]];

nreps = 1000;
seed = 4533;
repsave = all;
save = mc_ [[nobsmmin]]_ [[nobsmmax]]_*.dat;

ANALYSIS:
type = mixture;
algorithm = integration;

processors = 2;
```

```
MODEL POPULATION:
%OVERALL%

i s q | y1@0 y2@1 y3@2 y4@3;
i ON qft*-0.101;
s ON qft*-0.228;
q ON qft*0.131;

i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*0.313];

[i*73.050 s*8.125 q*-2.161];
i*67.887; s*64 q*3.958;
y1*52.956 y2*64.049 y3*55.481 y4*19.390;

%g#1%

i s q | y1@0 y2@1 y3@2 y4@3;
i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*0.313];

[i*73.050 s*8.125 q*-2.161];

%g#2%

i s q | y1@0 y2@1 y3@2 y4@3;
i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*2.704];

[i*71.541 s*6.525 q*-2.161];

OUTPUT: TECH9;
```

# Syntax data generation (32,000 data files)

---

```
[[init]]
iterators = nobsmmin nobsmmax;

nobsmmin = 5 10 25 50;
nobsmmax = 50 100 200 500 1000 2000 5000 10000;
filename = "[[nobsmmin]]-[[nobsmmax]].inp";

outputDirectory = "C:/Sim/S[[nobsmmin]]/data";
[[/init]]

TITLE: Linear Growth MC

MONTECARLO:
NAMES = y1-y4 qft;
!y1-y4 = cognition, qft = alcohol use
count = qft;
generate = qft(c);
ngroups = 2;
nobs = [[nobsmmax]] [[nobsmmin]];

nreps = 1000;
seed = 4533;
repsave = all;
save = mc_[[nobsmmin]]_[[nobsmmax]]_*.dat;

ANALYSIS:
type = mixture;
algorithm = integration;

processors = 2;

ACTION:

0 y2@1 y3@2 y4@3;
.101;
.228;
131;
3.669 q*12.342;
4.052;

;
*8.125 q*-2.161];
*64 q*3.958;
y1*52.956 y2*64.049 y3*55.481 y4*19.390;

%g#1%

i s q | y1@0 y2@1 y3@2 y4@3;
i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*0.313];

[i*73.050 s*8.125 q*-2.161];

%g#2%

i s q | y1@0 y2@1 y3@2 y4@3;
i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*2.704];

[i*71.541 s*6.525 q*-2.161];

OUTPUT: TECH9;
```

# Syntax data generation (32,000 data files)

---

```
[[init]]
iterators = nobsmmin nobsmmax;

nobsmmin = 5 10 25 50;
nobsmmax = 50 100 200 500 1000 2000 5000 10000;
filename = "[[nobsmmin]]-[[nobsmmax]].inp";

outputDirectory = "C:/Sim/S[[nobsmmin]]/data";
[[/init]]
```

TITLE: Linear Growth MC

```
MONTECARLO:
NAMES = y1-y4 qft;
!y1-y4 = cognition, qft = alcohol use
count = qft;
generate = qft(c);
ngroups = 2;
nobs = [[nobsmmax]] [[nobsmmin]];

nreps = 1000;
seed = 4533;
repsave = all;
save = mc_ [[nobsmmin]]_ [[nobsmmax]]_*.dat;

ANALYSIS:
type = mixture;
algorithm = integration;

processors = 2;
```

```
MODEL POPULATION:
%OVERALL%

i s q | y1@0 y2@1 y3@2 y4@3;
i ON qft*-0.101;
s ON qft*-0.228;
q ON qft*0.131;

i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*0.313];

[i*73.050 s*8.125 q*-2.161];
i*67.887; s*64 q*3.958;
y1*52.956 y2*64.049 y3*55.481 y4*19.390;

%g#1%

i s q | y1@0 y2@1 y3@2 y4@3;
i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*0.313];

[i*73.050 s*8.125 q*-2.161];

%g#2%

i s q | y1@0 y2@1 y3@2 y4@3;
i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*2.704];

[i*71.541 s*6.525 q*-2.161];

OUTPUT: TECH9;
```

# Syntax data generation (32,000 data files)

---

```
[[init]]
iterators = nobsmmin nobsmmax;

nobsmmin = 5 10 25 50;
nobsmmax = 50 100 200 500 1000 2000 5000 10000;
filename = "[[nobsmmin]]-[[nobsmmax]].inp";

outputDirectory = "C:/Sim/S[[nobsmmin]]/data";
[[/init]]

MONTECARLO:
NAMES = y1-y4 qft;
!y1-y4 = cognition, qft = alcohol use
count = qft;
generate = qft(c);
ngroups = 2;
nobs = [[nobsmmax]] [[nobsmmin]];

nreps = 1000;
seed = 4533;
repsave = all;
save = mc_ [[nobsmmin]]_ [[nobsmmax]]_*.dat;

ANALYSIS:
type = mixture;
algorithm = integration;

processors = 2;
```

```
MODEL POPULATION:
%OVERALL%

i s q | y1@0 y2@1 y3@2 y4@3;
i ON qft*-0.101;
s ON qft*-0.228;
q ON qft*0.131;

i with s*-53.669 q*12.342;
s with q*-14.052;

qft*0.313];

i*73.050 s*8.125 q*-2.161];
t*67.887; s*64 q*3.958;
l*52.956 y2*64.049 y3*55.481 y4*19.390;

j#1%

s q | y1@0 y2@1 y3@2 y4@3;
with s*-53.669 q*12.342;
with q*-14.052;

qft*0.313];

i*73.050 s*8.125 q*-2.161];

j#2%

s q | y1@0 y2@1 y3@2 y4@3;
with s*-53.669 q*12.342;
with q*-14.052;

qft*2.704];

i*71.541 s*6.525 q*-2.161];

JTPUT: TECH9;
```

# Syntax data generation (32,000 data files)

---

```
[[init]]
iterators = nobsmmin nobsmmax;

nobsmmin = 5 10 25 50;
nobsmmax = 50 100 200 500 1000 2000 5000 10000;
filename = "[[nobsmmin]]-[[nobsmmax]].inp";

outputDirectory = "C:/Sim/S[[nobsmmin]]/data";
[[/init]]
```

TITLE: Linear Growth MC

```
MONTECARLO:
NAMES = y1-y4 qft;
!y1-y4 = cognition, qft = alcohol use
count = qft;
generate = qft(c);
ngroups = 2;
nobs = [[nobsmmax]] [[nobsmmin]];

nreps = 1000;
seed = 4533;
repsave = all;
save = mc_ [[nobsmmin]]_ [[nobsmmax]]_*.dat;

ANALYSIS:
type = mixture;
algorithm = integration;

processors = 2;
```

```
MODEL POPULATION:
%OVERALL%

i s q | y1@0 y2@1 y3@2 y4@3;
i ON qft*-0.101;
s ON qft*-0.228;
q ON qft*0.131;

i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*0.313];

[i*73.050 s*8.125 q*-2.161];
i*67.887; s*64 q*3.958;
y1*52.956 y2*64.049 y3*55.481 y4*19.390;

%g#1%

i s q | y1@0 y2@1 y3@2 y4@3;
i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*0.313];

[i*73.050 s*8.125 q*-2.161];

%g#2%

i s q | y1@0 y2@1 y3@2 y4@3;
i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*2.704];

[i*71.541 s*6.525 q*-2.161];

OUTPUT: TECH9;
```

# Syntax data generation (32,000 data files)

## MODEL POPULATION:

### %OVERALL%

```
i s q | y1@0 y2@1 y3@2 y4@3;  
i ON qft*-0.101;  
s ON qft*-0.228;  
q ON qft*0.131;
```

```
i with s*-53.669 q*12.342;  
s with q*-14.052;
```

```
[qft*0.313];
```

```
[i*73.050 s*8.125 q*-2.161];  
i*67.887; s*64 q*3.958;  
y1*52.956 y2*64.049 y3*55.481  
y4*19.390;
```

### %g#1%

```
i s q | y1@0 y2@1 y3@2 y4@3;  
i with s*-53.669 q*12.342;  
s with q*-14.052;
```

```
[qft*0.313];
```

```
[i*73.050 s*8.125 q*-2.161];
```

### %g#2%

```
i s q | y1@0 y2@1 y3@2 y4@3;  
i with s*-53.669 q*12.342;  
s with q*-14.052;
```

```
[qft*2.704];
```

```
[i*71.541 s*6.525 q*-2.161];
```

OUTPUT: TECH9;



# Syntax Bayesian analysis (224 input files)

---

```
[[init]]
iterators = nobsmmin nobsmmax prior;
nobsmmin = 5 10 25 50;
nobsmmax = 50 100 200 500 1000 2000 5000 10000;

prior = 10000000000 5 2 1 0.4 0.5 0.3 0.1;
filename = "bayes[[nobsmmin]]prior[[prior]]-
[[nobsmmax]].inp";

outputDirectory = "C:/Sim/S[[nobsmmin]]/Bayes S/
bayesS[[nobsmmin]]prior[[prior]]";
[[/init]]
```

**TITLE:** Linear Growth MC

```
DATA:
FILE = "C:/Sim/S[[nobsmmin]]/Data/
mc_[[nobsmmin]]_[[nobsmmax]]_list.dat";
TYPE = MONTECARLO;
VARIABLE:
names = QFT Y1 Y2 Y3 Y4 G;
classes = cg(2);
knownclass is cg(g=1 g=2)
```

```
ANALYSIS: type = mixture;
ESTIMATOR = BAYES;
BCONVERGENCE = .05;
Chains=22;
Processors=22;

Biterations=(5000) 100000;
```

```
MODEL:
%OVERALL%
i s q | y1@0 y2@1 y3@2 y4@3;
i ON qft*-0.101;
s ON qft*-0.228;
q ON qft*0.131;

i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*0.313]; qft;

[i*73.050 s*8.125 q*-2.161];
i*67.887; s*64 q*3.958;

y1*52.956 y2*64.049 y3*55.481 y4*19.390;

%cg#1%
i s q | y1@0 y2@1 y3@2 y4@3;
[qft*0.313]; qft;
[i*73.050 s*8.125 q*-2.161] (I1 S1 Qg);

%cg#2%
i s q | y1@0 y2@1 y3@2 y4@3;
[qft*2.704]; qft;
[i*71.541 s*6.525 q*-2.161] (I2 S2 Qg);

MODEL PRIORS:
I1~N(73.050,[[prior]]);
S1~N(8.125,[[prior]]);
I2~N(71.541,[[prior]]);
S2~N(6.525,[[prior]]);
Qg~N(-2.161,[[prior]]);

MODEL CONSTRAINT:
NEW(diff_s)*1.6;
diff_s = S1 - S2;
```

# Syntax Bayesian analysis (224 input files)

---

```
[[init]]
iterators = nobsmin nobsmax prior;
nobsmin = 5 10 25 50;
nobsmax = 50 100 200 500 1000 2000 5000 10000;

prior = 10000000000 5 2 1 0.4 0.5 0.3 0.1;
filename = "bayes[[nobsmin]]prior[[prior]]-[[nobsmax]].inp";

outputDirectory = "C:/Sim/S[[nobsmin]]/Bayes S/bayesS[[nobsmin]]prior[[prior]]";
[/init]]

DATA:
FILE = "C:/Sim/S[[nobsmin]]/Data/
mc_ [[nobsmin]]_ [[nobsmax]]_list.dat";
TYPE = MONTECARLO;
VARIABLE:
names = QFT Y1 Y2 Y3 Y4 G;
classes = cg(2);
knownclass is cg(g=1 g=2)

ANALYSIS: type = mixture;
ESTIMATOR = BAYES;
BCONVERGENCE = .05;
Chains=22;
Processors=22;

Biterations=(5000) 100000;

%cg#1%
i s q | y1@0 y2@1 y3@2 y4@3;
[qft*0.313]; qft;
[i*73.050 s*8.125 q*-2.161] (I1 S1 Qg);

%cg#2%
i s q | y1@0 y2@1 y3@2 y4@3;
[qft*2.704]; qft;
[i*71.541 s*6.525 q*-2.161] (I2 S2 Qg);

MODEL PRIORS:
I1~N(73.050, [[prior]]);
S1~N(8.125, [[prior]]);
I2~N(71.541, [[prior]]);
S2~N(6.525, [[prior]]);
Qg~N(-2.161, [[prior]]);

MODEL CONSTRAINT:
NEW(diff_s)*1.6;
diff_s = S1 - S2;
```

# Syntax Bayesian analysis (224 input files)

---

```
[[init]]
iterators = nobsmmin nobsmmax prior;
nobsmmin = 5 10 25 50;
nobsmmax = 50 100 200 500 1000 2000 5000 10000;

prior = 10000000000 5 2 1 0.4 0.5 0.3 0.1;
filename = "bayes[[nobsmmin]]prior[[prior]]-
[[nobsmmax]].inp";

outputDirectory = "C:/Sim/S[[nobsmmin]]/Bayes S/
bayesS[[nobsmmin]]prior[[prior]]";
[[/init]]
```

**TITLE:** Linear Growth MC

```
DATA:
FILE = "C:/Sim/S[[nobsmmin]]/Data/
mc_[[nobsmmin]]_[[nobsmmax]]_list.dat";
TYPE = MONTECARLO;
VARIABLE:
names = QFT Y1 Y2 Y3 Y4 G;
classes = cg(2);
knownclass is cg(g=1 g=2)
```

```
ANALYSIS: type = mixture;
ESTIMATOR = BAYES;
BCONVERGENCE = .05;
Chains=22;
Processors=22;

Biterations=(5000) 100000;
```

```
MODEL:
%OVERALL%
i s q | y1@0 y2@1 y3@2 y4@3;
i ON qft*-0.101;
s ON qft*-0.228;
q ON qft*0.131;

i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*0.313]; qft;

[i*73.050 s*8.125 q*-2.161];
i*67.887; s*64 q*3.958;

y1*52.956 y2*64.049 y3*55.481 y4*19.390;

%cg#1%
i s q | y1@0 y2@1 y3@2 y4@3;
[qft*0.313]; qft;
[i*73.050 s*8.125 q*-2.161] (I1 S1 Qg);

%cg#2%
i s q | y1@0 y2@1 y3@2 y4@3;
[qft*2.704]; qft;
[i*71.541 s*6.525 q*-2.161] (I2 S2 Qg);

MODEL PRIORS:
I1~N(73.050,[[prior]]);
S1~N(8.125,[[prior]]);
I2~N(71.541,[[prior]]);
S2~N(6.525,[[prior]]);
Qg~N(-2.161,[[prior]]);

MODEL CONSTRAINT:
NEW(diff_s)*1.6;
diff_s = S1 - S2;
```

# Syntax Bayesian analysis (224 input files)

---

```
[[init]]
iterators = nobsmmin nobsmmax prior;
nobsmmin = 5 10 25 50;
nobsmmax = 50 100 200 500 1000 2000 5000 10000;

prior = 10000000000 5 2 1 0.4 0.5 0.3 0.1;
filename = "bayes[[nobsmmin]]prior[[prior]]-
[[nobsmmax]].inp";

outputDirectory = "C:/Sim/S[[nobsmmin]]/Bayes S/
bayesS[[nobsmmin]]prior[[prior]]";
[[/init]]
```

**TITLE: Linear Growth MC**

**DATA:**

**FILE = "C:/Sim/S[[nobsmmin]]/Data/mc\_[[nobsmmin]]\_[[nobsmmax]]\_list.dat";**

**TYPE = MONTECARLO;**

**VARIABLE:**

**names = QFT Y1 Y2 Y3 Y4 G;**

**classes = cg(2);**

**knownclass is cg(g=1 g=2)**

**ANALYSIS: type = mixture;**

**ESTIMATOR = BAYES;**

**BCONVERGENCE = .05;**

**Chains=22;**

**Processors=22;**

**Bit iterations=(5000) 100000;**

```
MODEL:
%OVERALL%
i s q | y1@0 y2@1 y3@2 y4@3;
i ON qft*-0.101;
s ON qft*-0.228;
q ON qft*0.131;

i with s*-53.669 q*12.342;
s with q*-14.052;

[qft*0.313]; qft;
```

# Syntax Bayesian analysis (224 input files)

---

**MODEL:**

**%OVERALL%**

```
i s q | y1@0 y2@1 y3@2 y4@3;
```

```
i ON qft*-0.101;
```

```
s ON qft*-0.228;
```

```
q ON qft*0.131;
```

```
i with s*-53.669 q*12.342;
```

```
s with q*-14.052;
```

```
[qft*0.313]; qft;
```

```
[i*73.050 s*8.125 q*-2.161];
```

```
i*67.887; s*64 q*3.958;
```

```
y1*52.956 y2*64.049 y3*55.481 y4*19.390;
```

**%cg#1%**

```
i s q | y1@0 y2@1 y3@2 y4@3;
```

```
[qft*0.313]; qft;
```

```
[i*73.050 s*8.125 q*-2.161] (I1 S1 Qg);
```

**%cg#2%**

```
i s q | y1@0 y2@1 y3@2 y4@3;
```

```
[qft*2.704]; qft;
```

```
[i*71.541 s*6.525 q*-2.161] (I2 S2 Qg);
```

**MODEL PRIORS:**

```
I1~N(73.050, [[prior]]);
```

```
S1~N(8.125, [[prior]]);
```

```
I2~N(71.541, [[prior]]);
```

```
S2~N(6.525, [[prior]]);
```

```
Qg~N(-2.161, [[prior]]);
```

**MODEL CONSTRAINT:**

```
NEW(diff_s)*1.6;
```

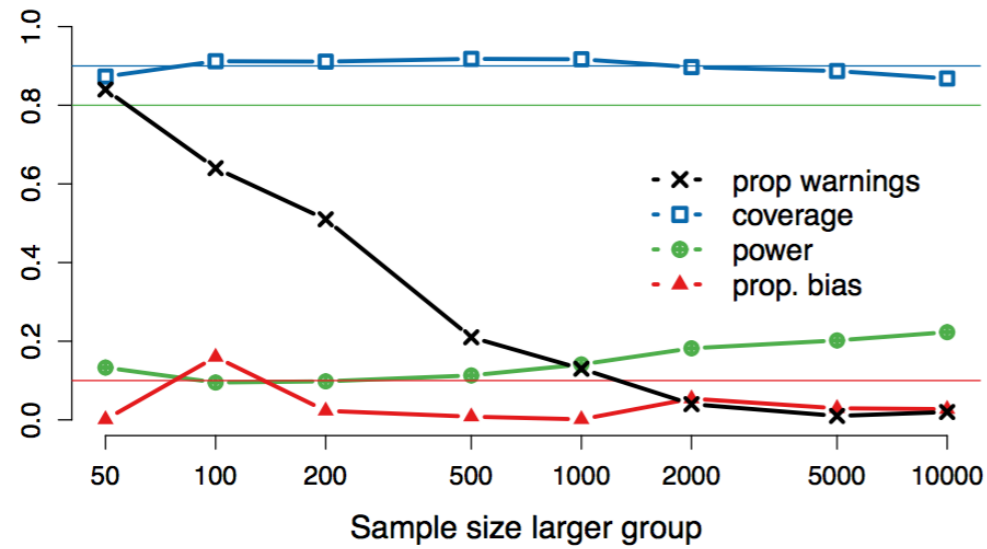
```
diff_s = S1 - S2;
```

# Simulation evaluation

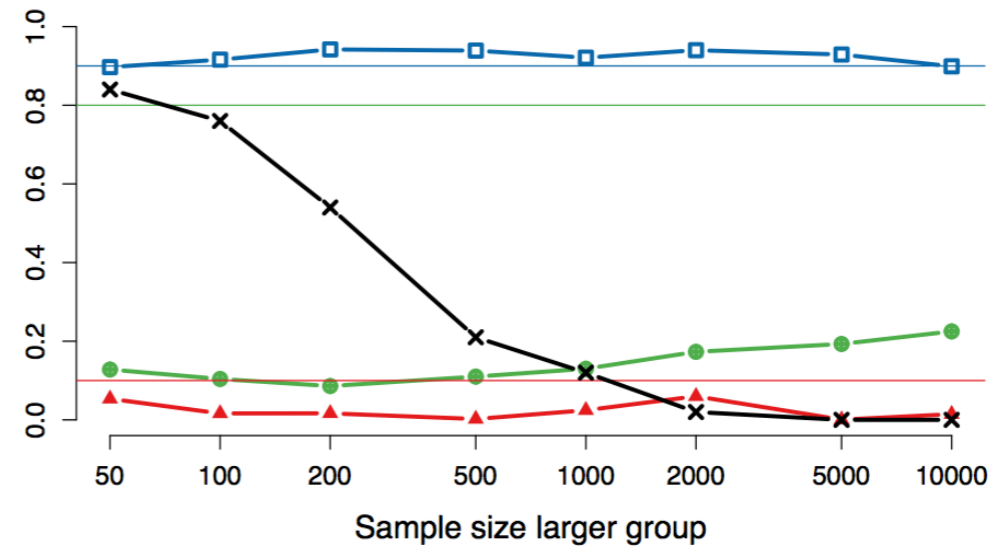
---

- Relative bias  $(\leq .10)$   
 $(\Delta\mathbf{a}_{2\_pop} - \Delta\mathbf{a}_{2\_est}) / \Delta\mathbf{a}_{2\_pop}$
- Coverage  $(\geq .90)$   
%  $\Delta\mathbf{a}_{2\_pop}$  in 95% interval of  $\Delta\mathbf{a}_{2\_est}$
- Power to detect a small effect  $(\geq .80)$   
% statistically sign.  $\Delta\mathbf{a}_{2\_est}$
- Estimation problems  $(\approx 0)$   
proportion of warnings, problems with convergence

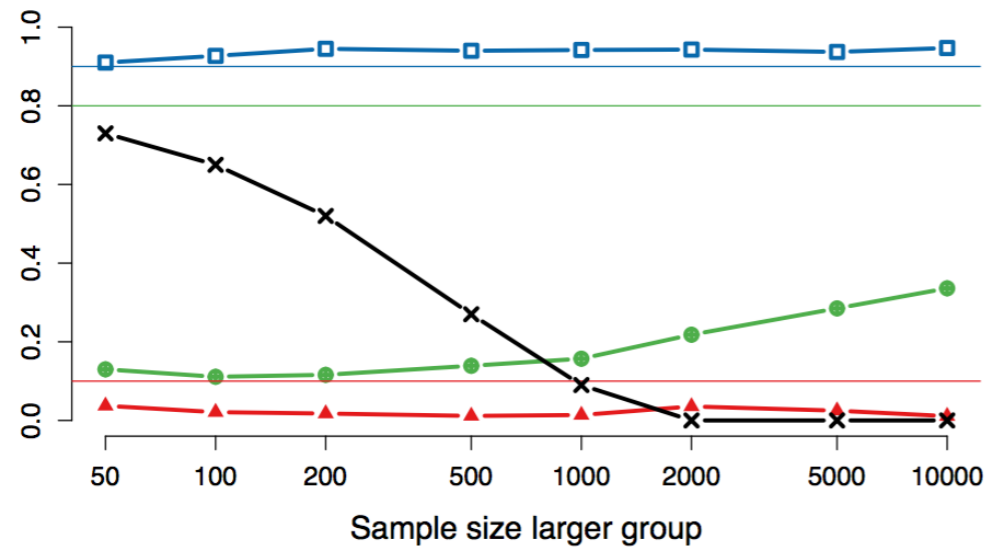
# Results ML estimation



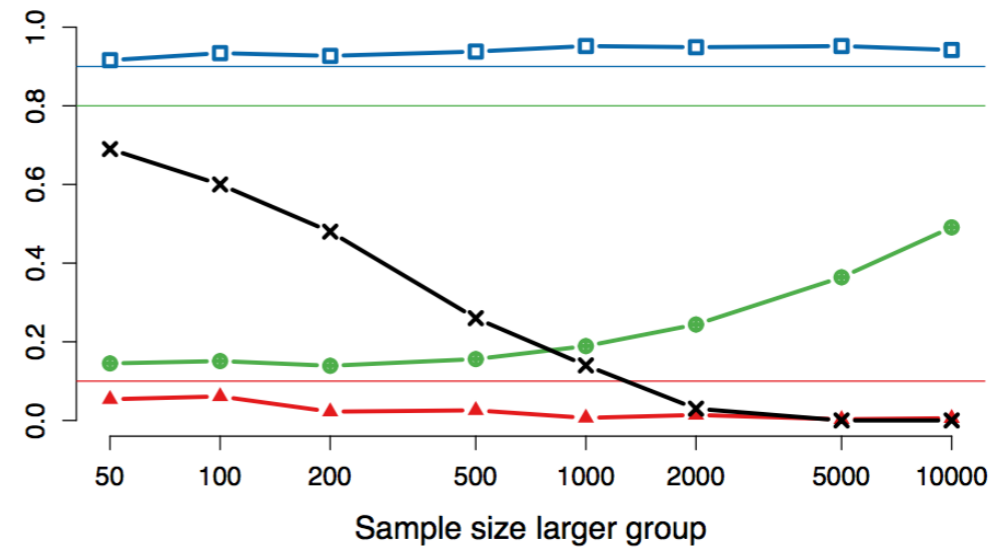
(a)  $n = 5$



(b)  $n = 10$



(c)  $n = 25$

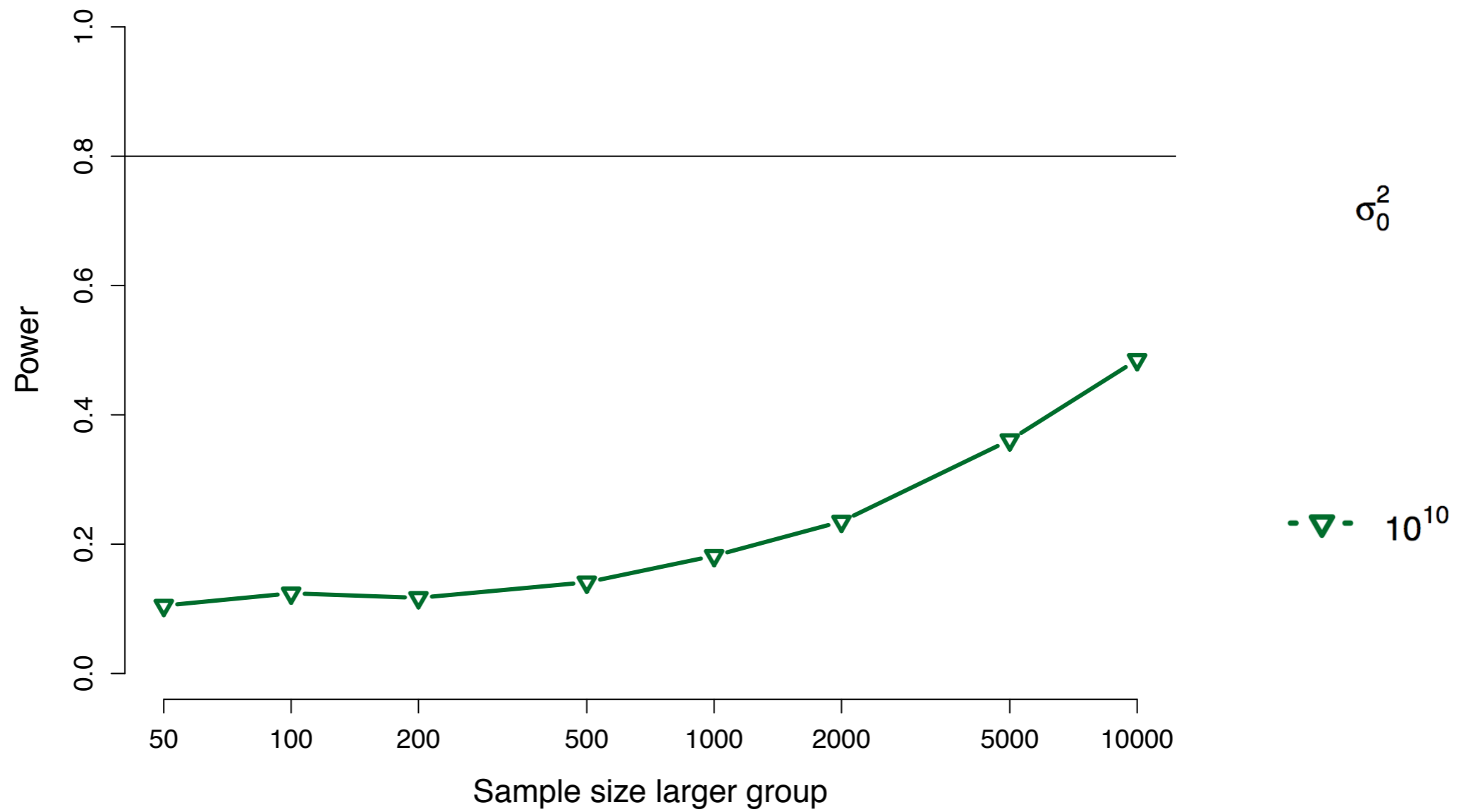


(d)  $n = 50$

Figure 1. Results for ML estimation by exceptional group sample size.

# Results Bayesian estimation

---

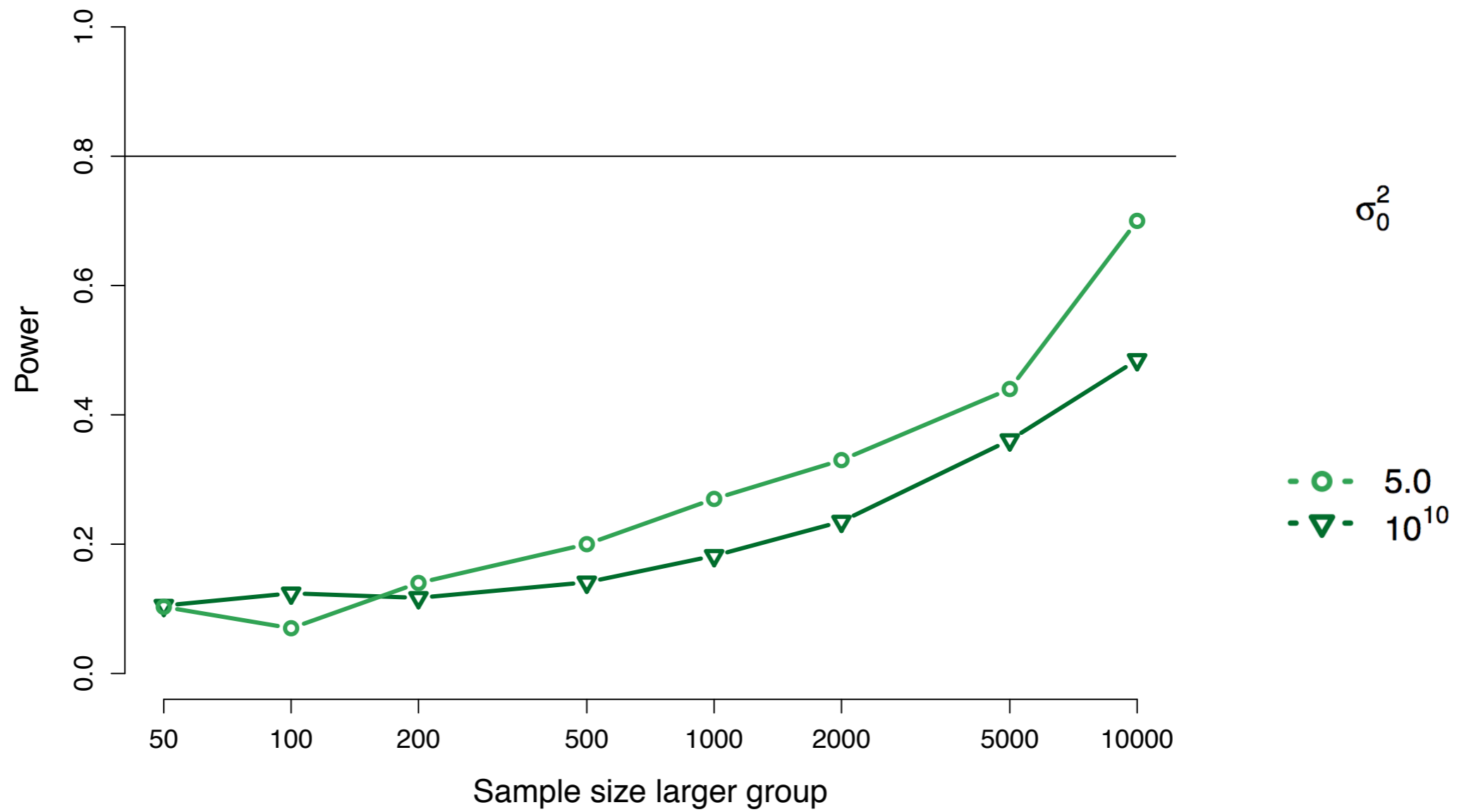


(d)  $n = 50$



# Results Bayesian estimation

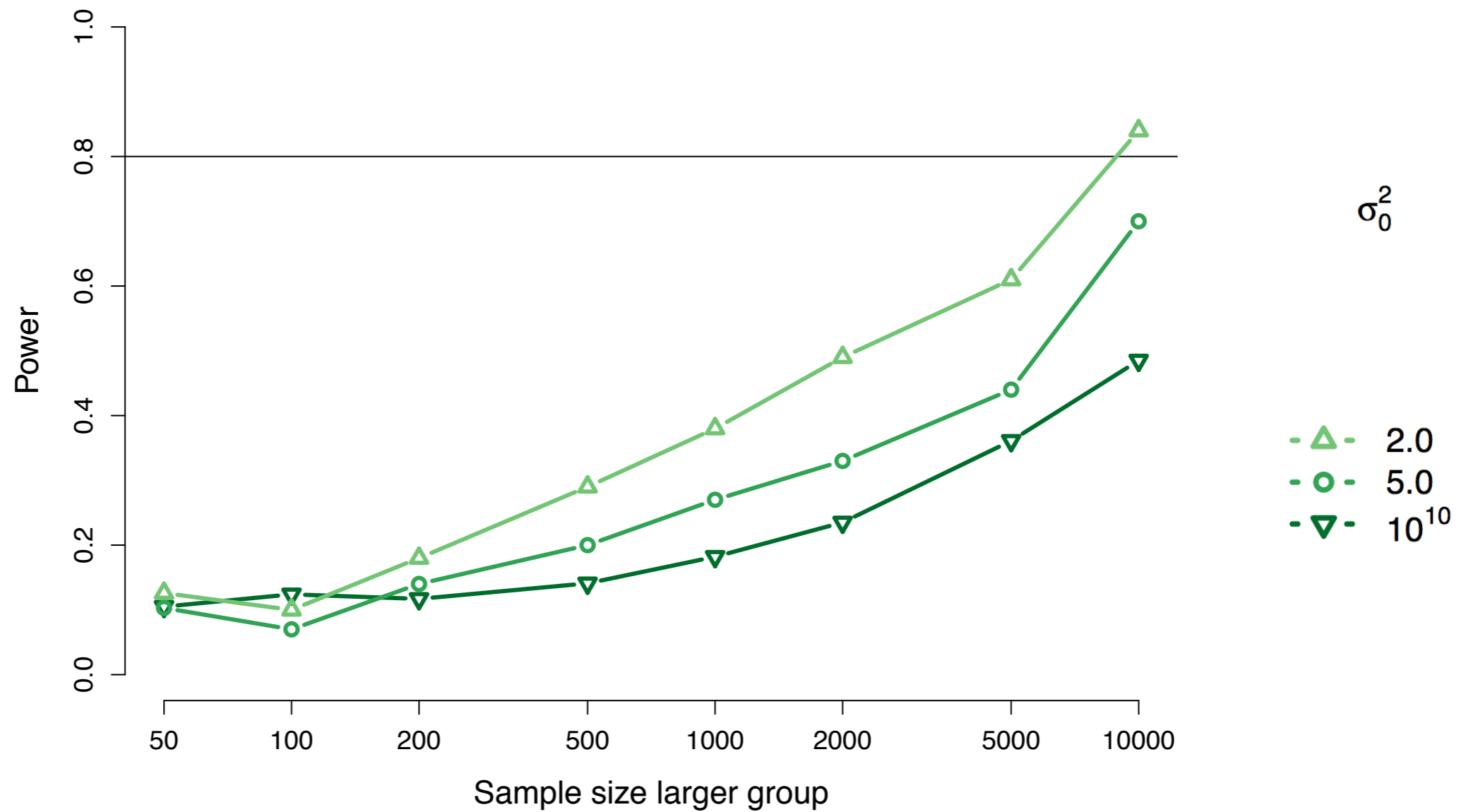
---



(d)  $n = 50$

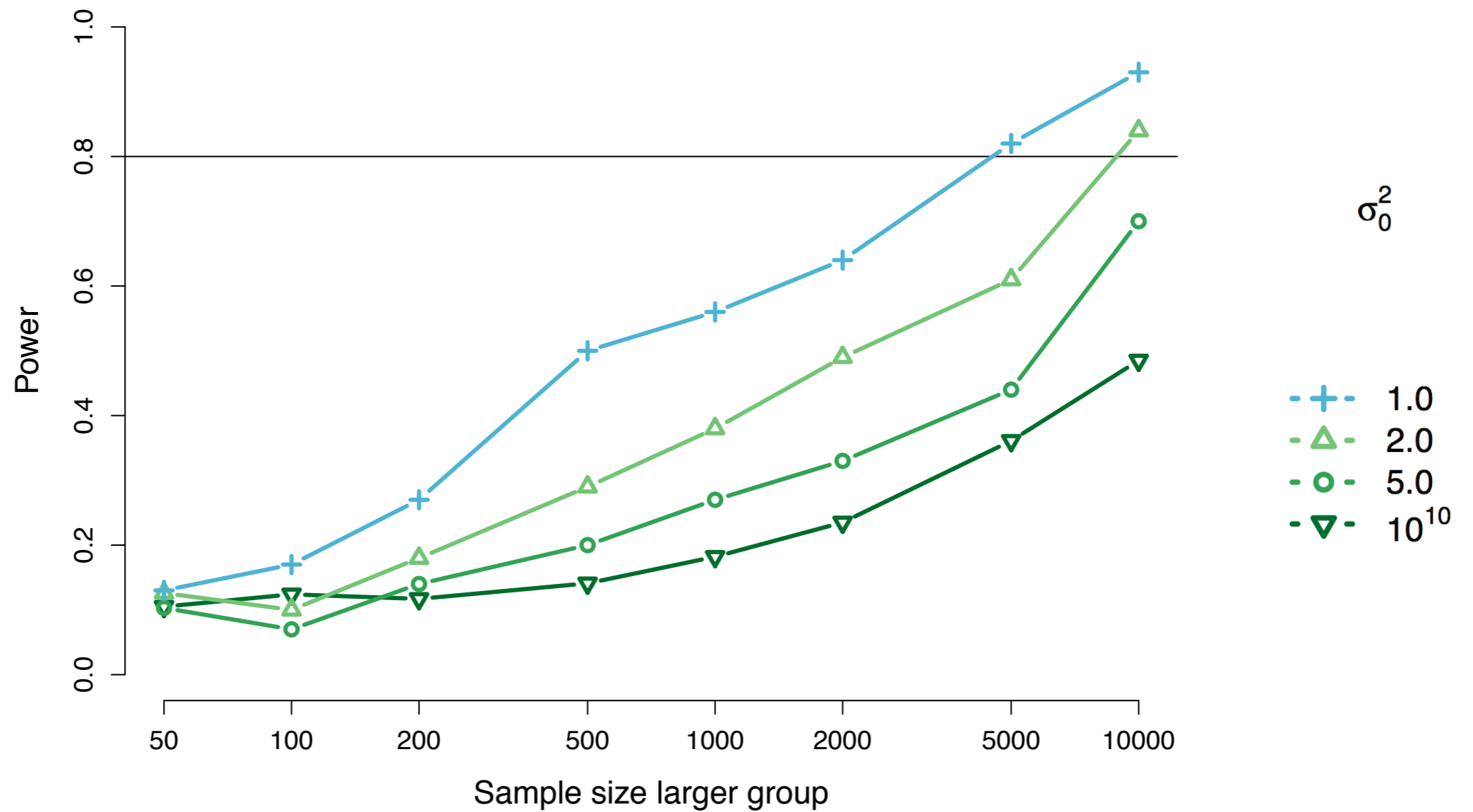
# Results Bayesian estimation

---



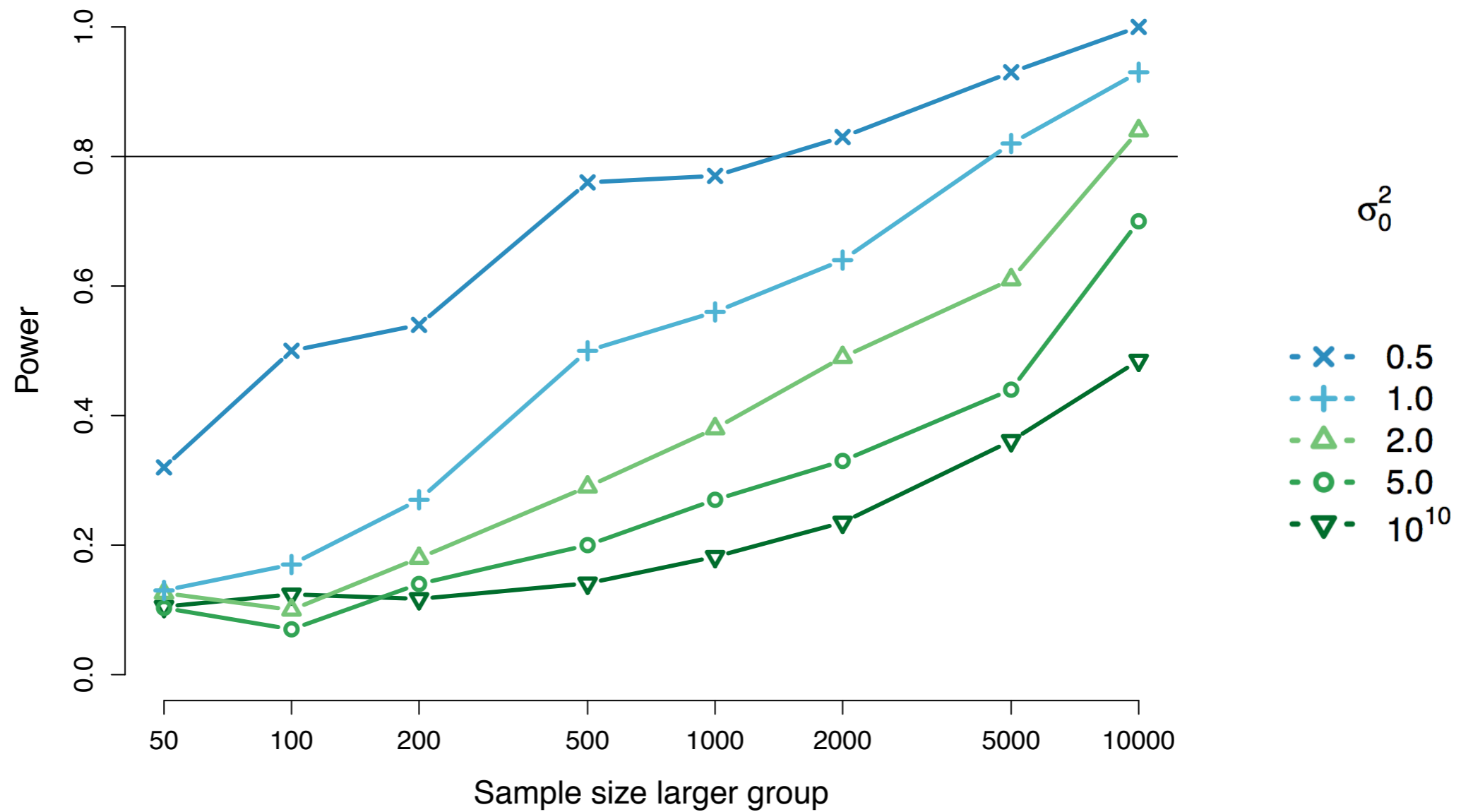
(d)  $n = 50$

# Results Bayesian estimation



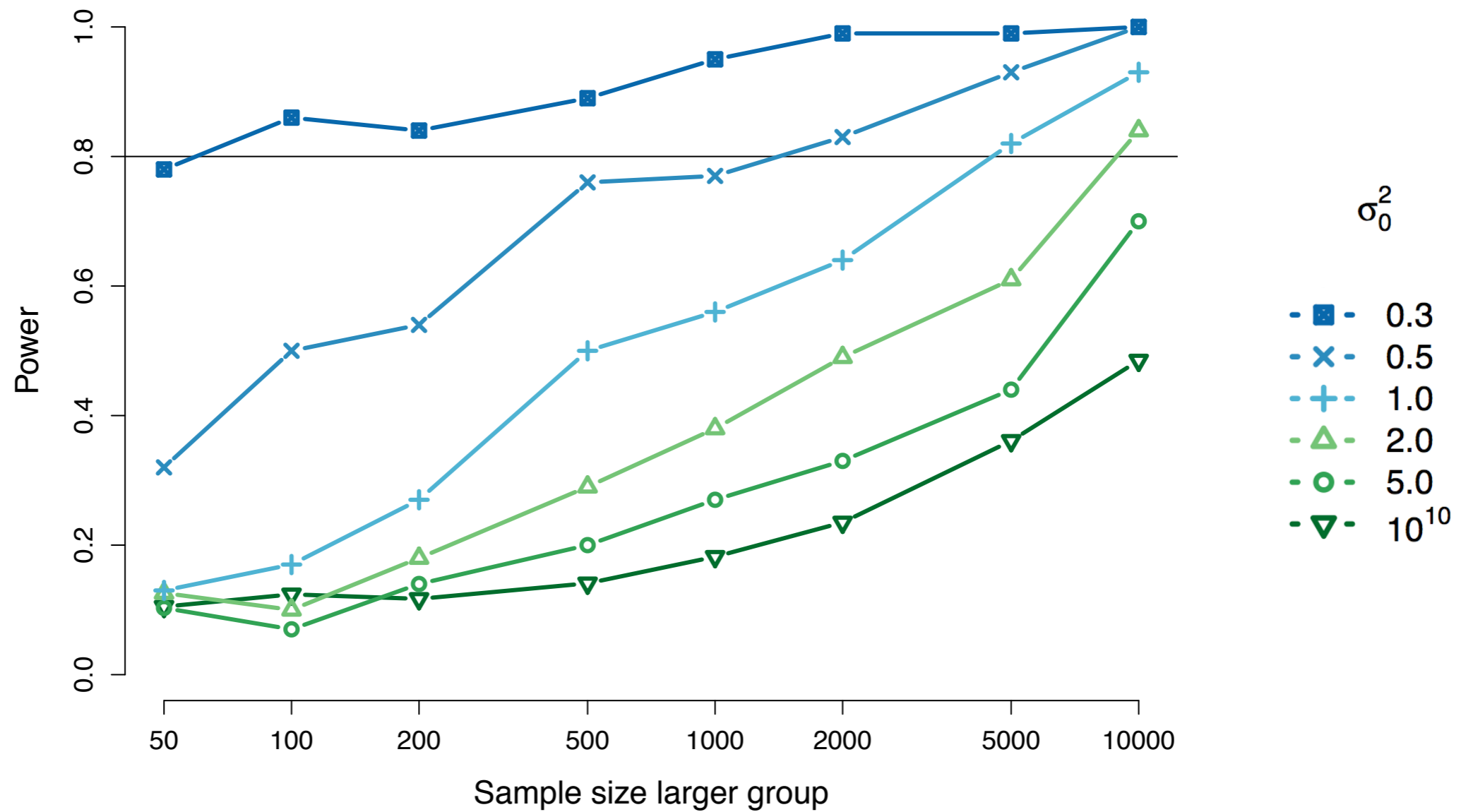
(d)  $n = 50$

# Results Bayesian estimation



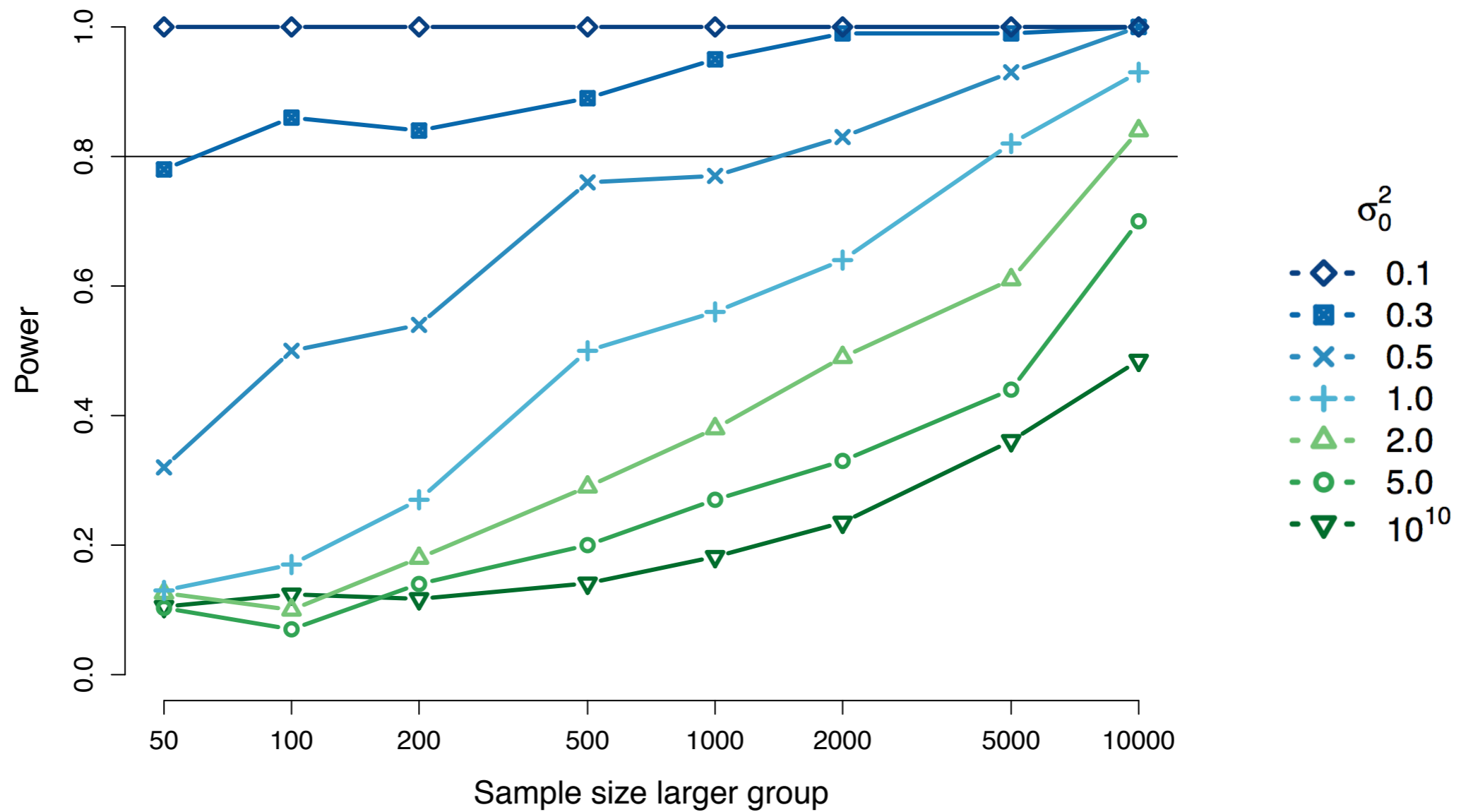
(d)  $n = 50$

# Results Bayesian estimation



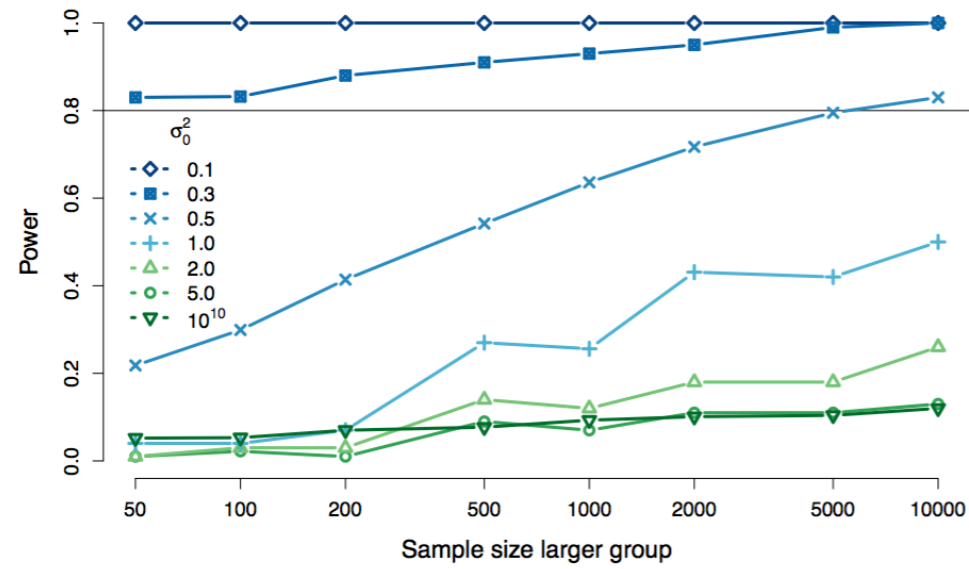
(d)  $n = 50$

# Results Bayesian estimation

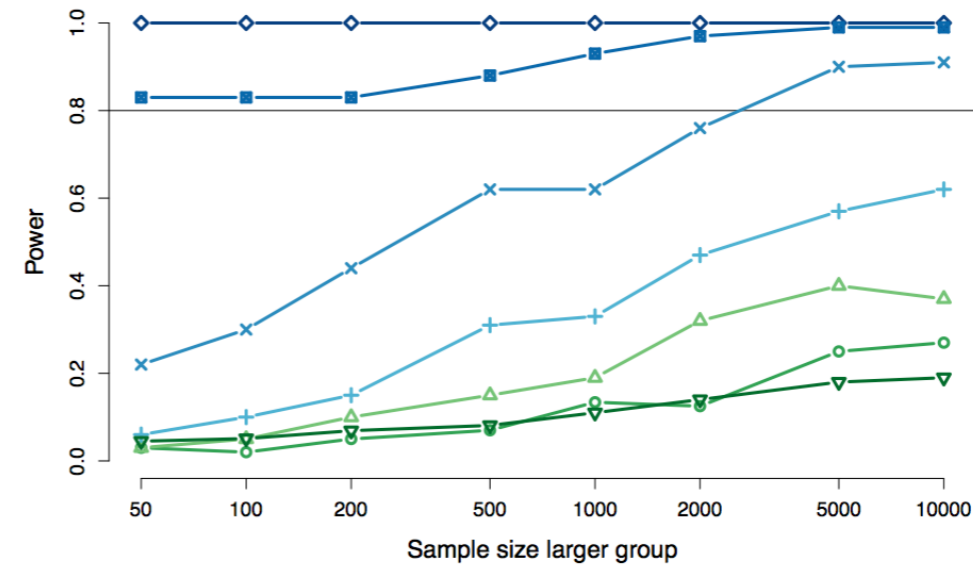


(d)  $n = 50$

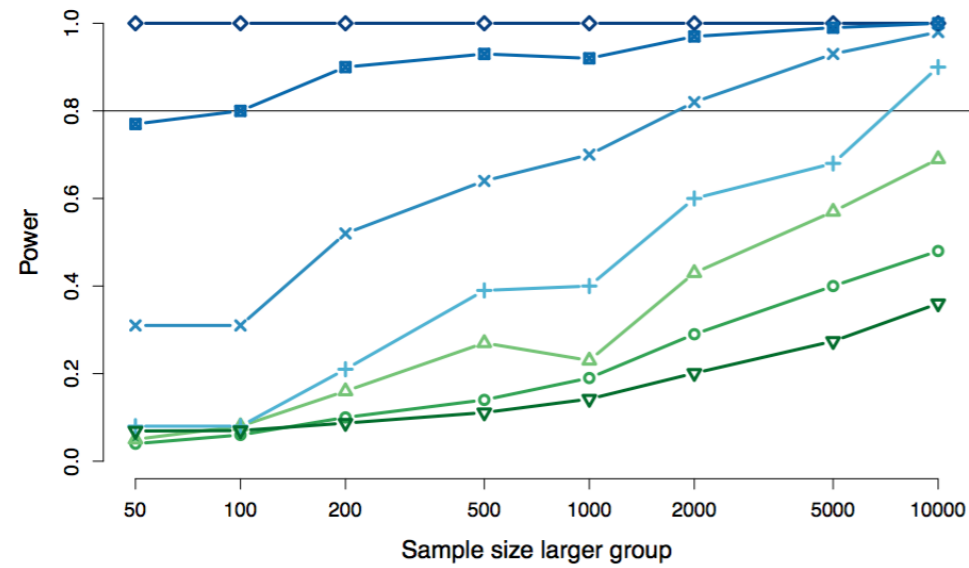
# Results Bayesian estimation



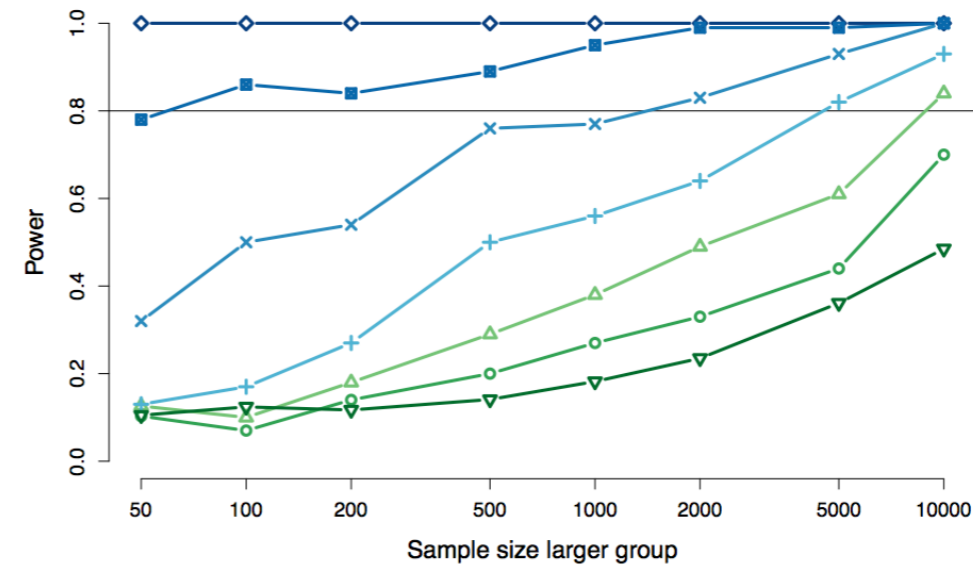
(a)  $n = 5$



(b)  $n = 10$



(c)  $n = 25$



(d)  $n = 50$

Figure 2. Power for Bayesian estimation by exceptional group sample size.

# Overview & Conclusion

---

- ML  
bias: ✓, coverage: ✓, estimation issues: ✗, power: ✗



# Overview & Conclusion

---

- ML  
bias: ✓, coverage: ✓, estimation issues: ✗, power: ✗
- Bayes default  
bias: ✓, coverage: ✓, estimation issues: ✓, power: ✗

# Overview & Conclusion

---

- ML  
bias: ✓, coverage: ✓, estimation issues: ✗, power: ✗
- Bayes default  
bias: ✓, coverage: ✓, estimation issues: ✓, power: ✗
- Bayes informative  
bias: ✓, coverage: ✓, estimation issues: ✓, power: ✓

# To be continued

---

Is it that easy?

## Reference

Zondervan-Zwijnenburg, M. A. J., Peeters, M., Vollebergh, W. A. M., Van de Schoot, R. (2014). Pushing the limits: Sample size requirements with unbalanced subgroups in latent growth models. Unpublished master's thesis. Utrecht University, The Netherlands.

# To be continued

---

Is it that easy?

→ Friday 12:05 am, Ruppert Rood

## Reference

Zondervan-Zwijnenburg, M. A. J., Peeters, M., Vollebergh, W. A. M., Van de Schoot, R. (2014). Pushing the limits: Sample size requirements with unbalanced subgroups in latent growth models. Unpublished master's thesis. Utrecht University, The Netherlands.

# To be continued

---

Is it that easy?

→ Friday 12:05 am, Ruppert Rood

## Questions

### Reference

Zondervan-Zwijnenburg, M. A. J., Peeters, M., Vollebergh, W. A. M., Van de Schoot, R. (2014). Pushing the limits: Sample size requirements with unbalanced subgroups in latent growth models. Unpublished master's thesis. Utrecht University, The Netherlands.